

B.Tech II Year I Semester (R09) Supplementary Examinations December 2015

ELECTROMAGNETIC WAVES & TRANSMISSION LINES

(Electronics & Instrumentation Engineering)

Time: 3 hours

Max. Marks: 70

Answer any FIVE questions
All questions carry equal marks

- 1 (a) State and prove Gauss's law. Give three applications of Gauss's law with suitable examples.
(b) Given that electric flux density $D = z \rho \cos^2 \phi a_z \text{ C/m}^2$, use Gauss's law to calculate the charge density at $(1, \pi/4, 3)$ and the total charge enclosed by the cylinder of radius of 1 m with $-2 \leq z \leq 2$.
- 2 (a) Determine magnetic field intensity H at any point in free space due to any straight filamentary conductor of finite length directed along z - axis.
(b) A circular loop located on $x^2 + y^2 = 9, z = 0$ carries a direct current of 10 A along a_ϕ . Determine magnetic field intensity H at $(0, 0, 4)$ and $(0, 0, -4)$.
- 3 (a) What are the boundary conditions of the magnetic field? Explain.
(b) Medium 1 ($z < 0$) is filled with a material whose relative permeability is six, and medium 2 ($z > 0$) is filled with a material whose relative permeability is 4. If the interface carries current of $a_y/\mu_0 \text{ mA/m}$, and $B_2 = 5a_x + 8a_z \text{ mWb/m}^2$, find H_1 and B_1 .
- 4 (a) Prove that for a good conductor, the intrinsic impedance of a plane wave $\eta = (1 + j)/(\sigma\delta)$.
(b) A lossy dielectric has an intrinsic impedance of 200 ohms magnitude and phase of 30° at a particular frequency. If at that frequency, the plane wave propagating through the dielectric has the magnetic field component $H = 10 \exp(-ax) \cos(\omega t - 0.5x) a_y \text{ A/m}$, find E and skin depth.
- 5 (a) State and prove the Poynting's theorem with regard to EM wave propagation.
(b) A uniform plane wave in air with $H = 4 \sin(\omega t - 5x) a_y \text{ A/m}$ is normally incident on a plastic region with parameters $\epsilon = 4\epsilon_0, \mu = \mu_0, \sigma = 0$. Obtain the total electric field in air and calculate the time average power density in the plastic region.
- 6 (a) Obtain expressions for the cut-off frequency and phase velocity in the rectangular waveguide starting from the field expressions of TE modes.
(b) A rectangular air-filled waveguide has a cross section of 80 x 40 mm. Find cut-off wavelength for dominant mode. How many modes are passed at 2.5 times cut-off frequency?
- 7 (a) Derive the expression for characteristic impedance of a transmission line in terms of primary constants of the line.
(b) A telephone line has $R = 30 \text{ ohms/km}, L = 100 \text{ mH/km}, C = 20 \text{ } \mu\text{F/km}$, and $G = 0$. At frequency of 1 kHz, determine the characteristic impedance of the line, the propagation constant and the phase velocity.
- 8 (a) Show that a lossy transmission line of length ' l ' has an input impedance of $Z_0 \tanh \gamma l$ when it is shorted and $Z_0 \coth \gamma l$ when it is open at the load end.
(b) A quarter-wave lossless 100 ohm line is terminated by a load of 210 ohms. If the voltage at the receiving end is 80 V, what is the voltage at the sending end?
