B.Tech II Year I Semester (R09) Supplementary Examinations December 2015 PROBABILITY \& STATISTICS
(Common to CSE \& MCT)
Time: 3 hours
Max. Marks: 70
Answer any FIVE questions
All questions carry equal marks
1 A person writes letters to six friends and addresses the corresponding envelops. What is the probability that the letter be placed in the envelops so that:
(a) At least two of them are in the wrong envelops.
(b) All the letters in the wrong envelops.

2 If the probability density of a random variable is given by $f(x)=K\left(1-x^{2}\right)$ for, $0<x<1=0$ elsewhere. Find the value of $K$ and the probabilities that a random variable will take a value:
(a) Between . 1 and .2.
(b) Greater than .5.

3 If X is the number appearing on a die when it is thrown, show that the Chebyshev's theorem gives $P(|X-\mu|>2.5)<0.47$. While the actual probability is zero.

4 Find $P(\bar{x}>66.75)$ if a random sample of size 36 is drawn from an infinite population with mean $\mu=63$ and $s . . d \sigma=9$.

5 (a) Define unbiased estimator. What is more efficient unbiased estimator? Explain briefly.
(b) Show that $\bar{x}$ is an unbiased estimator of the population mean $\mu$.

6 (a) Write a note on one tailed test and two tailed test?
(b) The mean life time of a sample of 100 light tubes produced by a company is found to be 1560 hours with a population S.D. of 90 hours. Test the hypothesis for $\alpha=0.05$ that the mean life time of the light tubes produced by the company is 1580 hours.
$7 \quad$ Fit a Poisson distribution to the following data and test the goodness of the fit at $\alpha=0.05$ level of significance.

8 (a) Write about (M/M/1) : ( $\infty / F I F O)$ Queuing system.
(b) Derive the formula for the probability distribution density function of the waiting time distribution.

