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B.Tech II Year I Semester (R13) Regular & Supplementary Examinations December 2015

PROBABILITY THEORY & STOCHASTIC PROCESSES

(Electronics and Communication Engineering)

Time: 3 hours

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Max. Marks: 70

PART – A

(Compulsory Question)

- Answer the following: (10 X 02 = 20 Marks)
 - (a) What are the conditions to be satisfied for the statistical independence of three events A, B and C?
 - (b) Show that $P(x_1 < X \le x_2) = F_X(x_2) F_X(x_1)$.
 - (c) Two random variables X and Y have the following values:

$$E[X] = E[Y] = \frac{7}{12}, E[XY] = \frac{1}{3}$$
 and $\sigma_X = \sigma_Y = \sqrt{\frac{11}{144}}$. Find the correlation coefficient.

- (d) Define the joint moments about the origin.
- (e) Define WSS random process.
- (f) Determine the mean-square value of a random process with autocorrelation function: $R_{XX}(\tau) = e^{-|\tau|}$.
- (g) A random process has the power density spectrum $S_{XX}(\omega) = \frac{6\omega^2}{1+\omega^4}$. Find the average power in the process.
- (h) Define rms bandwidth of the power spectrum.
- (i) Impulse response of a linear system is h(t) = [1 t][u(t) u(t 1)]. The input to this system is a sample function from a random process having an autocorrelation function of $R_{XX}(\tau) = \delta(\tau)$. Find the autocorrelation of the output.
- (j) A stationary random process with a mean of 2 is passed through an LTI system with $h(t) = 2e^{-2t} u(t)$. Determine the mean of the output process.

- 2 (a) Define conditional distribution and density functions and list their properties.
 - (b) A continuous random variable X has a PDF $f_X(x) = 3x^2$, $0 \le x \le 1$. Find 'a' and 'b' such that: (i) $P\{X \le a\} = P\{X > a\}$. (ii) $P\{X > b\} = 0.05$.

OR

- 3 (a) Define random variable and give the concept of random variable with an example.
 - (b) The probability density function of a random variable has the form $f_X(x) = 5e^{-kx}u(x)$, where u(x) is the unit step function. Find the probability that X > 1.

UNIT – II

4 (a) Define marginal density and distribution functions.

(b) Let X and Y be jointly continuous random variables with joint probability density function:

 $f_{XY}(x, y) = x^{2} + \frac{xy}{3}; \quad 0 \le x \le 1, 0 \le y \le 2$ = 0 ; elsewhere

Find: (i) $f_X(x)$. (ii) $f_Y(y)$. (iii) Are X and Y independent?

OR

- 5 (a) State central limit theorem for the following two cases:(i) Equal distributions. (ii) Unequal distributions.
 - (b) Let $f_{XY}(x, y) = 4x + 2y$, $0 \le x \le 1/2$, $0 \le y \le 1$ and zero elsewhere. Find $P\{X \le 1/4\}$.

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UNIT – III

A random process has sample functions of the form: $X(t) = \begin{cases} A; & 0 \le t \le 1 \\ 0; & else where \end{cases}$ 6 (a) Where A is a random variable uniformly distributed from 0 to 10. Find the autocorrelation function of this process.

(b) Show that $|R_{XX}(\tau)| \le R_{XX}(0)$.

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OR

- 7 (a) Show that the autocorrelation function of a stationary random process is an even function of τ .
 - (b) Give the classification of random processes.

UNIT – IV

(a) A stationary random process has a two-sided spectral density given by: 8

 $S_{XX}(f) = \begin{cases} 10; & a < |f| < b \\ 0; & else \ where \end{cases}$ Find the mean-square value of the process if a = 4 and b = 5.

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(b) List the properties of power spectral density function.

OR

- 9 (a) For two jointly stationary random processes, the cross-correlation function is $R_{XY}(\tau) = 2e^{-2\tau}u(\tau)$. Find the two cross-spectral density function.
 - List the properties of cross power spectral density function. (b)

10 Show that $R_{YY}(\tau) = R_{XX}(\tau) * h(\tau) * h(-\tau)$.

OR

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- 11 Write short notes on the following:
 - Bandpass random process. (a)
 - Band-limited random process. (b)