

B.Tech III Year II Semester (R13) Regular Examinations May/June 2016

FINITE ELEMENT METHODS IN ENGINEERING

(Civil Engineering)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

- 1 Answer the following: (10 X 02 = 20 Marks)
- List out advantages of FEM.
 - Define plane stress with a suitable example.
 - Differentiate between global and local axes.
 - What is geometric invariance?
 - What are the properties of stiffness matrix?
 - What is shape function and state their properties?
 - Define Iso-parametric element and state their purpose.
 - What is an Axi symmetric element and state usage?
 - What is static condensation?
 - Write about solution technique for static loads.

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

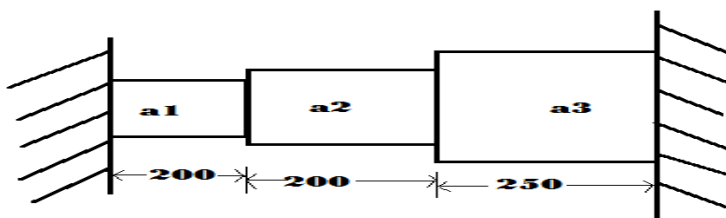
- 2 (a) Explain the different steps involved in FEM.
(b) Find out deflection at centre of a simply supported beam of span length (l) subjected to uniformly distributed load throughout its length of intensity w per unit length. Use Rayleigh Ritz method. Take EI is constant.

OR

- 3 (a) Write about stress-strain relationship in matrix form for a plane stress element.
(b) If a displacement field is described by $u = (x^2 - 2y^2 + 6xy)10^{-4}$ and $v = (6x + 3y)10^{-4}$, Determine ϵ_x , ϵ_y and γ_{xy} at the point $x = 2$ and $y = 1$.

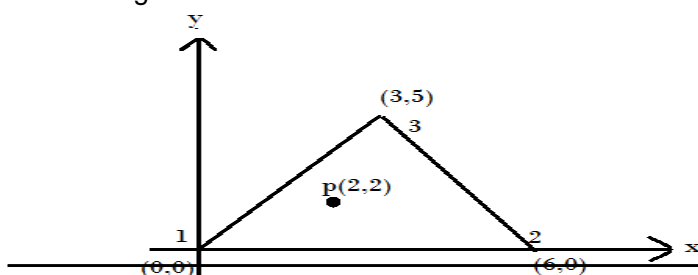
UNIT – II

- 4 For the stepped bar shown in the figure below, determine the nodal displacements, element stress and support reactions. Take $P = 500$ kN, $E = 210$ GPa, $a_1 = 200$ mm², $a_2 = 300$ mm² and $a_3 = 500$ mm².



OR

- 5 (a) Differentiate between CST and LST elements.
(b) Evaluate the shape functions N_1 , N_2 and N_3 at the interior point P for the triangular element shown in the figure below.



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UNIT – III

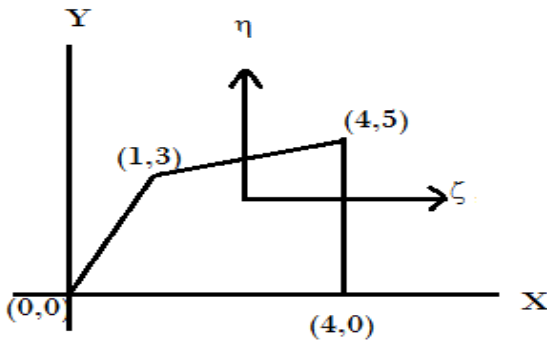
- 6 Determine the stiffness matrix, for the plane stress element as shown in figure above. Take $E = 200 \text{ GPa}$, and $\mu = 0.3$, thickness of element = 10 mm.

OR

- 7 (a) Determine the shape functions for a constant strain triangular element using area co-ordinates.
(b) Derive the strain-displacement matrix (B-matrix) for plane stress analysis of three node triangular element.

UNIT – IV

- 8 Evaluate the Jacobian matrix at the local co-ordinates ζ, η are (0, 0) for the element shown in the below.



OR

- 9 The nodal co-ordinates for an axisymmetric triangular element are given as: $r_1 = 0$, $r_2 = 25$, $r_3 = 30$, $z_1 = 0$, $z_2 = 0$ and $z_3 = 40 \text{ mm}$ respectively. Determine the strain-displacement matrix for the element.

UNIT – V

- 10 (a) What is meant by Newton-Cotes Numerical integration?
(b) Write briefly about "Gauss –Quadrature method".

OR

- 11 Evaluate the Integral $I = \int_{-1}^1 (3e^x + x^2 + \frac{1}{(x+2)})$ using one point and two point Gauss quadrature. Compare this with exact solution
