

Code: 9A02709

B.Tech IV Year I Semester (R09) Supplementary Examinations June 2017

OPTIMIZATION TECHNIQUES
(Electrical & Electronics Engineering)

Time: 3 hours

Max. Marks: 70

Answer any FIVE questions
All questions carry equal marks

- 1 (a) What is the difference between constraint surface and composite constraint surface?
(b) State five engineering applications of optimization.
- 2 (a) Determine the maximum and minimum values of the function: $f(x) = 12x^5 - 45x^4 + 40x^3 + 5$.
(b) Find the dimensions of a cylindrical tin (with top and bottom) made up of sheet metal to maximize its volume such that the total surface area is equal to $A_0 = 24\pi$.

- 3 Solve the following system of equations using pivot operations.

$$6x_1 - 2x_2 + 3x_3 = 11$$

$$4x_1 + 7x_2 + x_3 = 21$$

$$5x_1 + 8x_2 + 9x_3 = 48$$

- 4 Determine an initial feasible solution to the following transportation problem by VAM method and test for its optimality.

		Destination			Supply units
		D ₁	D ₂	D ₃	
Source	S ₁	2	8	12	20
	S ₂	10	6	18	29
	S ₃	12	5	4	40
	S ₄	3	2	8	25
Demand (units)		30	20	15	

- 5 (a) Find the minimum of $f = x(x - 1.5)$ by starting from (0, 0) with an initial step size of 0.05.
(b) Derive the one-dimensional minimization problem for the following case. $Min f(x) = (x_1^2 - x_2)^2 + (1 - x_1)^2$, from the starting point $x_1 = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$ along the search direction $S = \begin{bmatrix} 1.00 \\ 0.25 \end{bmatrix}$

- 6 Minimize $f(x_1, x_2) = x_1 - x_2 + 2x_1^2 + 2x_1x_2 + x_2^2$ starting from the point $x = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$.

- 7 Minimize $f(x_1, x_2) = \frac{1}{3}(x_1 + 1)^3 + x_2$, subject to $g_1(x_1, x_2) = -x_1 + 1 \leq 0$, $g_2(x_1, x_2) = -x_2 \leq 0$

- 8 Solve the following problem by dynamic programming

$$Max. \sum_{i=1}^3 d_i^2$$

Subject to $d_i = x_{i+1} - x_i$, $i = 1, 2, 3$

$x_i = 0, 1, 2, \dots, 5$, $i = 1, 2$

$x_3 = 5$, $x_4 = 0$.
