

B.Tech II Year I Semester (R13) Supplementary Examinations June 2017

SIGNALS & SYSTEMS

(Common to ECE and EIE)

Time: 3 hours

Max. Marks: 70

PART – A

(Compulsory Question)

- 1 Answer the following: (10 X 02 = 20 Marks)
- Find the even and odd components of the following signal $x(t) = \cos t + \sin t + \sin t \cos t$.
 - What are the conditions for a system to be LTI system?
 - Write short notes on Dirichlets conditions for Fourier series.
 - State and prove symmetry property of Fourier series.
 - Explain how Aperiodic signals can be represented by Fourier transform.
 - State convolution property in relation to Fourier transform.
 - State sampling theorem.
 - Give the system impulse response $h(t)$. State the conditions for stability and causality.
 - State modulation property and multiplication in Fourier transform.
 - What are the properties of ROC in z transform?

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

- 2 (a) Consider a rectangular pulse as shown by the equation $x(t) = \begin{cases} A; & -0.5 < t < 0.5 \\ 0; & \text{otherwise} \end{cases}$. Express $x(t)$ as a weighted sum of two step functions.
- (b) Explain the various operations on signals.

OR

- 3 (a) Write the Classification of systems based on certain properties.
- (b) The I order system is described by the following difference equation $y[n] = ay[n-1] + x[n]$ and has the impulse response $h[n] = a^n u[n]$. Is this system casual, memory less or BIBO stable?

UNIT – II

- 4 (a) Find the Fourier series for $|x|$, $-\pi < x < \pi$.
- (b) Find the exponential form of the Fourier series for the signal $x(t) = 2 + 4 \sin\left(\frac{1}{2}t + \frac{\pi}{6}\right) + 3 \cos\left(\frac{3}{5}t - \frac{\pi}{4}\right)$

OR

- 5 (a) Find the cosine Fourier series of a half wave rectified sine function.
- (b) State and prove convolution property in Fourier series.

UNIT – III

- 6 (a) Determine Fourier transform of an impulse train.
- $$x(t) = \sum_n \delta(t - nT).$$
- (b) Determine DTFT of the following signal: $x(n) = 4(2^n) u(n)$. Find the magnitude.

OR

- 7 (a) Find the inverse DTFT of $X(e^{jw}) = 2\sin 2w$, $-\pi < w < \pi$.
- (b) Determine CTFT of the following signal. $x(t) = \begin{cases} A; & \text{for } -\tau/2 \leq t \leq \tau/2 \\ 0; & \text{elsewhere} \end{cases}$

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UNIT – IV

- 8 The input and output of a causal LTI system are related by the differential equation:

$$d^2y(t)/dt^2 + 6dy(t)/dt + 8y(t) = 2x(t)$$

(i) Find the impulse response of the system.

(ii) What is the response of this system if $x(t) = t e^{-2t} u(t)$

OR

- 9 Compute & plot the convolution $y(t)$ of the given signals:

(i) $X(t) = u(t-3) - u(t-5)$, $h(t) = u(t)$.

(ii) $X(t) = u(t)$, $h(t) = u(t)$.

UNIT – V

- 10 The system function of the LTI system is given as $H(Z) = (3-4(Z^{-1})) / (1 - 3.5Z^{-1} + 1.5Z^{-2})$. Specify the ROC of $H(Z)$ and determine $h(n)$ for the following condition: (i) Stable system. (ii) Causal system.

OR

- 11 A system is described by the differential equation:

$$d^2y(t)/dt^2 + 3dy(t)/dt + 2y(t) = dx(t)/dt \text{ if } y(0) = 2; dy(0)/dt = 1 \text{ and } x(t) = e^{-t} u(t)$$

Use Laplace transform to determine the response of the system to a unit step input applied at $t = 0$.
