



Max. Marks: 70

B.Tech II Year I Semester (R13) Supplementary Examinations June 2017 MATHEMATICS – III

(Common to EEE, ECE and EIE)

Time: 3 hours

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PART – A

(Compulsory Question)

- Answer the following: (10 X 02 = 20 Marks)
 - (a) Write any two properties of beta function.
 - (b) Compute the value of $\Gamma(-1/2)$.
 - (c) Show that $p_1(x) = x$.
 - (d) State the orthogonal property of Bessels differential equation.
 - (e) Check whether $u(x, y) = \sin x$ coshy is harmonic function.
 - (f) Discuss about a Transformation w = z + c, where 'c' is complex constant.
 - (g) Evaluate $\int_{C} e^{z} dz$ where C is |z| = 1.
 - (h) Expand $f(z) = e^{z}$ in Taylor's series about z = 1.

(i) Find the residue at z =1 of the function
$$f(z) = \frac{z^2}{(z-1)(z-2)^2}$$

(j) State Cauchy's residue theorem.

PART - B
(Answer all five units, 5 X 10 = 50 Marks)
UNIT - I
2 (a) Prove that
$$\int_{0}^{\infty} x^{n-1} e^{-kx} dx = \frac{\Gamma n}{k^{n}} (n > 0, k > 0).$$
(b) Prove that
$$\int_{0}^{\frac{\pi}{2}} Sin^{2m-1}\theta \cos^{2n-1}\theta d\theta = \frac{\beta(m, n)}{2}.$$
OR
3 Solve in Series the equation $x\frac{d^{2}y}{dx^{2}} + \frac{dy}{dx} + xy = 0$
UNIT - II
4 (a) Prove that $\frac{d}{dx}[xJ_{n}(x)J_{n+1}(x)] = x[J_{n}^{2}(x) - J_{n+1}^{2}(x)].$
(b) Express $J_{5}(x)$ in terms of $J_{0}(x)$ and $J_{1}(x)$.
OR

5 State and prove the Rodrigues formula of Legendre Polynomials.

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UNIT – III

- 6 (a) State and prove the Cauchy- Riemann equations in polar form.
 - (b) If f(z) = u + iv is Analytic function of z, find f(z) if $2u + v = e^{2x} [(2x + y)\cos 2y + (x 2y)\sin 2y]$ OR
- 7 (a) Find the bilinear Transformation which maps the points $z = \infty$, *i*, 0 into the points w = -1, -i, 1.
 - (b) Discuss about the Transformation $w = z^2$

UNIT – IV

- 8 (a) Evaluate $\int_{c} \frac{\sin^2 z}{\left(z \frac{\pi}{6}\right)^3} dz$, where c is the circle |z| = 1.
 - (b) Verify cauchy's theorem for the integral of z^3 taken over the boundary of the rectangle with vertices -1, 1, 1+i, -1+i
- 9 Find the Laurent series expansion of $\frac{z^2 6z 1}{(z 1)(z 3)(z + 2)}$ in the region 3 < |z + 2| < 5

UNIT – V

- 10 (a) Evaluate $\int_{c} \frac{dz}{(z^2+4)^2}$, using residue theorem, where c: |z-i|=2
 - (b) Determine the Residue of the function $f(z) = \frac{z+1}{z^2(z-2)}$ at each pole. OR Show that $\int_{0}^{2\pi} \frac{\cos 2\theta}{1-2a\cos\theta+a^2} = \frac{2\pi a^2}{1-a^2}$ where $a^2 < 1$
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