Code: 9A14501
B.Tech III Year I Semester (R09) Supplementary Examinations June 2017

NUMERICAL METHODS
(Mechatronics)
Time: 3 hours
Answer any FIVE questions
All questions carry equal marks
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1 (a) Find the root of the equation $x^{3}-2 x-5=0$ which lies near $x=2$.
(b) Find a real root of the equation $x=e^{-x}$, using the Newton-Raphson method.

2 (a) Solve the system of equations by Jacobi's iteration method.
$14 x_{1}-3 x_{2}=8: \quad x_{1}+5 x_{2}=11$
(b) Use Gauss-Seidal iteration method to solve the system.
$10 x+y+z=12$
$2 x+10 y+z=13$
$2 x+2 y+10 z=14$

3 (a) Find the Newton's forward difference interpolating polynomial for the data

| $x$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 1 | 3 | 7 | 13 |

(b) Given $x=1,2,3,4$ and $f(x)=1,2,9,28$ respectively find $f(3.5)$ using Lagrange method.

4 (a) Fit a polynomial of second degree to the data points given in the following table:

| $x$ | 0 | 1.0 | 2.0 |
| :---: | :---: | :---: | :---: |
| $y$ | 1.0 | 6.0 | 17.0 |

(b) Fit the exponential curve $\mathrm{y}=\mathrm{ae}{ }^{\mathrm{bx}}$ to the following data.

| $\mathrm{x}:$ | 2 | 4 | 6 | 8 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Y}:$ | 25 | 38 | 56 | 84 |

Evaluate $\int_{0}^{1} \sqrt{1+x^{3}} d x$ taking $\mathrm{h}=0.1$ using
(a) Simson's $1 / 3$ rule.
(b) Trapezoidal rule.

6 Obtain the values of $y$ at $x=0.1,0.2$ using Runge-Kutta method of:
(i) Second order.
(ii) Third order. (iii) Fourth order.

Find the Eigen values and the corresponding Eigen vectors of $A=\left[\begin{array}{ccc}-2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0\end{array}\right]$.
Find the values of $u(x, y)$ satisfying the Laplace's equation $\nabla^{2} u=0$ at the pivotal points of a square region with boundary values as shown in the following figure.


