IV B.Tech I Semester Examinations,NOVEMBER 2010 CHEMICAL ENGINEERING MATHEMATICS

Chemical Engineering
Time: 3 hours

## Answer any FIVE Questions

All Questions carry equal marks

1. Solve the system of equations by SOR method

$$
\left[\begin{array}{ccc}
4 & 0 & 2  \tag{16}\\
0 & 5 & 2 \\
5 & 4 & 10
\end{array}\right]\left[\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right]=\left[\begin{array}{c}
4 \\
-3 \\
2
\end{array}\right]
$$

2. The following heat transfer data is expected to follow a functional form of $\mathrm{Nu}=\mathrm{a}$ $(R e)^{b}$ where Nu is Nusselt number and Re is Reynolds number. Obtain the best value for the constants 'a' and 'b' by the method of averages

| Re | 12 | 20 | 30 | 40 | 100 | 300 | 400 | 1000 | 3000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nu | 2.0 | 2.5 | 3.0 | 3.3 | 5.3 | 10 | 11 | 17 | 30 |

3. Initially a tank contains 500 Kg of salt solution containing $10 \%$ salt. A stream containing $20 \%$ salt enters the tank at a flow rate of $10 \mathrm{Kg} / \mathrm{h}$. The stream leaving the tank has a constant flow rate of $5 \mathrm{Kg} / \mathrm{h}$. The tank is well stirred. Derive an equation relating the amount of the salt in the tank at any time $t$ in hours. Solve the differential equation.
4. (a) Solve $2 x^{2} \frac{d^{2} y}{d x^{2}}+y^{2}=x^{2}\left(\frac{d y}{d x}\right)^{2}$
(b) $\frac{d^{2} y}{d x^{2}}-5 \frac{d y}{d x}+6 y=0$
5. Solve the difference equation $Y_{n+2}-4 Y_{n+1}+3 Y_{n}=5^{n}$
6. Describe the application of finite difference method, for the calculation of number of stages required for a counter - current liquid-liquid extraction system.
7. In an experimental study of the safonification of ethyl acetate by sodium hydroxide, it is found that $30 \%$ of the ester is converted to alcohol in 15 min when the initial concentrations of both ester and caustic are 0.02 m . what conversion of ester would be obtained in one hour if the initial ester concentration were 0.030 m and the initial caustic concentration 0.02 m .
8. Write on factorial and fractional factorial methods of designing of experiments.

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1. (a) If $\mathrm{Z}=\mathrm{f}(\mathrm{x}, \mathrm{y})$ and $\mathrm{x}=\mathrm{r} \cos \pi$, $\mathrm{y}=\mathrm{r} \sin \pi$, prove that $\left(\frac{\partial z}{\partial x}\right)^{2}+\left(\frac{\partial z}{\partial y}\right)^{2}=\left(\frac{\partial z}{\partial r}\right)^{2}+\frac{1}{r^{2}}\left(\frac{\partial z}{\partial \theta}\right)^{2}$
(b) If $T=\left(x^{2}+y^{2}+z^{2}\right)^{-1 / 2}$ show that $\nabla^{2} T=0$
2. (a) Explain about the classes of second order differential equations.
(b) Solve $\frac{d^{2} y}{d x^{2}}-4 \frac{d y}{d x}+4 y=4 x+8 x^{3}$
3. (a) Write about the formulation of differential equation of physical problem.
(b) Discuss a flow process in which a precipitation is being carried out by mixing two streams A and B to form a third stream C in which the precipitate is carried away.
4. Use the method of averages to fit the best equation of the type $\mathrm{Nu}=\mathrm{a} \mathrm{Pr}^{n}$ to the following data.

| Pr | 0.74 | 4.2 | 5.6 | 3.0 | 5.0 | 10.0 | 17.7 | 18.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nu | 30.0 | 60.3 | 69.0 | 58.4 | 70.7 | 84.5 | 115 | 115 |

5. Explain about the design of experiments.
6. Solve the difference equation
$Y_{k+2}-2 Y_{k+1}+y_{k}=2^{k}$ with $Y_{0}=2$ and $Y_{1}(0)=1$.
7. Write short notes on:
(a) Calculation of number of plates required for an absorption column by finite difference method.
(b) Non-linear finite difference equations - Analytical solutions.
8. A process unit is fed with three liquid streams $\mathrm{A}, \mathrm{B}$, and C which separate out into two layers D and E. The compositions of the five streams in weight percent are as follows:

| Component | Steam |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E |
| 1 | 7 | 0 | 40 | 21 | 5 |
| 2 | 15 | 40 | 18 | 17 | 80 |
| 3 | 75 | 11 | 0 | 37 | 5 |
| 4 | 3 | 49 | 42 | 25 | 10 |

It is desired to find the quantities of raw materials A and C required and the quantity of products D and E produced per 1000 kg of B processed. Solve the problem using the Gauss Seidal method.

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Chemical Engineering
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1. If $\mathrm{Z}=\mathrm{f}(\mathrm{x}, \mathrm{y})$ and if $\mathrm{x}=\mathrm{u}-\nu, \mathrm{y}=\mathrm{u} \nu$, prove that
(a) $(u+v) \frac{\partial z}{\partial x}=u \frac{\partial z}{\partial u}-v \frac{\partial z}{\partial v}$
(b)

$$
(u+v) \frac{\partial z}{\partial y}=\frac{\partial z}{\partial u}+\frac{\partial z}{\partial v} \cdot v
$$

2. A boiling $100^{\circ} \mathrm{C}$ solution set on a table where room temperature to be constant at $20^{\circ} \mathrm{C}$ The solution cooled to $60^{\circ} \mathrm{C}$ after five minutes.
(a) Find a formula for the temperature ( T ) of the soluton, t min after it placed on the table.
(b) Determine how long time will take for the solution to cool to $22^{\circ} \mathrm{C}$. $[8+8]$
3. Calculate the least squares line and correlation coefficients for the following data:

| X | 89.16 | 84.16 | 74.79 | 86.47 | 82.87 | 57.77 | 79.07 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 3.98 | 4.94 | 6.47 | 3.75 | 4.99 | 7.09 | 4.79 |

4. An ammonia gas is absorbed by a solution with which it reacts chemically. the rate of diffusion in the liquid will be assumed proportional to the concentration difference with in the distance, the diffusing gas is reacted by first order kinetics and the rate of reaction is proportional to the concentration in the liquid. derive an expression for the concentration in the liquid as a function of distance from the interface.
5. A polymer blend is to be formed from three feed streams A, B and C having the following compositions in weight percent:

| Component | Steam |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | Blend |
| 1 | 25 | 35 | 55 | 30 |
| 2 | 35 | 20 | 40 | 30 |
| 3 | 40 | 45 | 5 | 40 |

Using Jacobi method determine the masses of A, B and C to produce 1000 kg of blend having the desired composition.
6. Explain the factorial method of designing of experiments.
7. A reactant A is to be converted into a product B in a battery of N continuous stirred tank reactors of total volume $\mathrm{V} \mathrm{m}^{3}$. If the feed rate is $\mathrm{q} \mathrm{m}^{3} / \mathrm{min}$ and the concentration of A is $C_{A 0}$. Show that the production of B is a maximum when all the tanks are the same size. The rate of reaction can be taken to be first order and the battery is to operate isothermally.
8. Solve the following difference equations:
(a) $\mathrm{Y}_{\mathrm{n}+2}-2 \mathrm{Y}_{\mathrm{n}} \operatorname{Cos} \alpha+\mathrm{Y}_{\mathrm{n}-1}=0$.
(b) $\mathrm{Y}_{\mathrm{n}+2}-5_{\mathrm{Yn}+1}-6 \mathrm{Y}_{\mathrm{n}}=2^{\mathrm{n}}$.


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Time: 3 hours
Max Marks: 80

## Answer any FIVE Questions

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1. (a) Explain about nonlinear and linear second order differential equations
(b) Solve $1.5 \frac{d^{2} y}{d x^{2}}-3 \frac{d y}{d x}=9$
2. Describe about the forward differences, backward differences and make the forward difference and backward difference tables.
3. Describe how finite difference method is applied for the calculation number of theoretical plates required for a distillation column. Illustrate with an example. [16]
4. Consider the rectangular fin. If the width of the fin is $W$ and the thickness is $2 B$, (a) convert the governing equation interms of $W$ and B (b) Introducing $V=\frac{T-T \infty}{T w-T \infty}$ and $Z=\frac{x}{L}$
Where $T_{W}=$ wall temperature , L $=$ Length of the fin $\frac{d^{2} V}{d Z^{2}}-M^{2} V=0$
Convert the differential equation into a dimensionless form:
5. The table below gives the temperature T in ${ }^{0} \mathrm{C}$ and length L in mm of a heated rod. If $L=a+b T$, find the best yalues of ' $a$ ' and ' $b$ ' by using the method of averages.

| $\mathrm{T}^{0} \mathrm{C}$ | 20 | 30 | 40 | 50 | 60 | 70 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~L}(\mathrm{~mm}):$ | 800.3 | 800.4 | 800.6 | 800.7 | 800.9 | 801.1 |

6. Analyse the following data obtained in a factorially designed experiment:

| Run | Conc.\% | Duration min. | Temp. ${ }^{0} \mathrm{C}$ | yield |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 87 | 15 | 60 | 6.08 |
| 2 | 93 | 15 | 60 | 6.04 |
| 3 | 87 | 30 | 60 | 6.53 |
| 4 | 93 | 30 | 60 | 6.43 |
| 5 | 87 | 15 | 70 | 6.79 |
| 6 | 93 | 15 | 70 | 6.68 |
| 7 | 87 | 30 | 70 | 6.73 |
| 8 | 93 | 30 | 70 | 6.18 |

7. A brass fin L m long is triangular in cross section. It is $\mathrm{x} m$ thick at the base and tapers off to a line. the base of this wedge shaped piece of metal is maintained at a constant temperature Tb , and the fin loses heat by the convection through the surrounding air which is at a temperature Ta, the surface coefficient of the heat transfer is $\mathrm{h} \mathrm{W} / \mathrm{hr} m 2^{\circ} \mathrm{C}$. What is the relation between the temperature of the fin metal, T , and the distance from the base L-k?
8. A settling tank is fed with three liquid streams $F_{1}, F_{2}$ and $F_{3}$ which separate out into two layers $P_{1}$ and $P_{2}$. The compositions of the five streams in weight percent are given below:

| Component | Steam |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | F1 | F2 | F3 | P1 | P2 |
| 1 | 21 | 0 | 62 | 5 | 15 |
| 2 | 18 | 41 | 16 | 80 | 5 |
| 3 | 36 | 10 | 0 | 3 | 75 |
| 4 | 25 | 49 | 22 | 12 | 5 |

It is desired to find the quantities of raw materials $F_{2}$ and $F_{3}$ required and Products $P_{1}$ and $P_{2}$ produced per 1000 kg of $F_{1}$ processed. Solve the problem using Gausssiedalmethod.
[16]

