## II B.TECH - I SEM EXAMINATIONS, NOVEMBER - 2010 PROBABILITY AND STATISTICS

Common to Information Technology, Computer Science And Engineering, Computer Science And Systems Engineering
Time: 3 hours
Max Marks: 80
Answer any FIVE Questions
All Questions carry equal marks

1. (a) A lady stenographer claims that she can take dictation at the rate of 118 words per minute can we reject her claim on the basis of 100 trials in which she demonstrates a mean of 116 words and a S.D of 15 words.
(b) In a large consignment of oranges a random sample of 64 oranges revealed that 14 oranges were bad. If it reasonable to ensure that $20 \%$ of the oranges are bad?
2. (a) Using recurrence formula find the probabilities when $x=0,1,2,3,4$ and 5 : If the mean of Poisson distribution is 3 .
(b) If the masses of 300 students are normally distributed with mean 68 kgs and standard deviation 3 kgs how many students have masses.
i. Greater then 72 kg
ii. Less than or equal to 64 kg
iii. Between 65 and 71 kg inclusive
3. The following is the distribution of hourly number of trucks arriving at a company's warehouse:

| No.of Trucks | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
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| Frequency | 52 | 151 | 130 | 102 | 45 | 12 | 5 | 1 | 2 |

Find the mean of this distribution, and using it as parameter $\lambda$, fit a Poisson distribution. Test for goodness of fit at the 0.05 level of significance?
4. (a) Calculate the coefficient of correlation for ranks if the marks in two subjects x and y are given below.
$(\mathrm{x}, \mathrm{y})=(5,8) ;(10,3) ;(6,2) ;(3,9) ;(19,12) ;(5,3) ;(6,17) ;(12,18) ;(8,22) ;(2,12) ;$ (10,17); $(19,20)$
(b) If $\mathrm{x}=2 \mathrm{y}+3$ and $\mathrm{y}=\mathrm{kx}+6$ are the regression lines of $\mathrm{x}, \mathrm{y}$ and y on x respectively
i. shown that $0 \leq \mathrm{k} \leq 1 / 2$
ii. If $\mathrm{k}=1 / 8$, find r and $(\bar{x}, \bar{y})$
5. (a) Find the most possible values of x and y from the following equations

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\begin{array}{ll}
x-5 y+4=0, & 2 x-3 y+5=0 \\
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(b) Fit a curve of the form $\mathrm{y}=a e^{b x}$ for the following data

| x | 1 | 2 | 3 | 4 | 5 | 6 |
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| y | 1.6 | 4.5 | 13.8 | 40.2 | 125 | 300 |

6. (a) If X and Y are discrete random variables and K is a constant then prove that.
i. $E(X+K)=E(X)+K$
ii. $\mathrm{E}(\mathrm{X}+\mathrm{Y})=\mathrm{E}(\mathrm{X})+\mathrm{E}(\mathrm{Y})$
(b) Out of 800 families with 5 childrens each, how many would you expect to have
i. 3 boys
ii. At least one boy.

$$
[8+8]
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7. (a) What is the probability that $X$ will be between 75 and 78 if a random sample of size 100 taken from an infinite population has, mean 76 and wariance 256 .
(b) Write about
i. Null hypothesis
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8. (a) If $A_{1}, A_{2}, \ldots \ldots \ldots$. An, are n events then prove that $\mathrm{P}\left(\bigcap_{i=1}^{n} A i\right) \geq \sum_{i=1}^{n} P(A i)-(n-1)$
(b) Companies $B_{1}, B_{2}, B_{3}$ produce $30 \%, 45 \%, 25 \%$ of the cars respectively. It is known that $2 \%, 3 \%, 2 \%$ of these cars produced from $B_{1}, B_{2}, B_{3}$ are defective.
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