III B.Tech I Semester Examinations,November 2010 FINITE ELEMENT MEHTODS

Mechatronics
Max Marks: 80
Time: 3 hours

1. If a displacement field is described as follows,

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\mathrm{u}=\left(-\mathrm{x}^{2}+2 y^{2}+6 x y\right) 10^{-4} \text { and } \mathrm{v}=\left(3 \mathrm{x}+6 \mathrm{y}-\mathrm{y}^{2}\right) 10^{-4}
$$

Determine the strain components $\epsilon_{x x}, \epsilon_{y y}$, and $\epsilon_{x y}$ at the point $\mathrm{x}=1, \mathrm{y}=0 .[16]$
2. Determine the displacement at node 1 of the truss structure as shown in the figure 2 :


Figure 2
3. Derive the elemental stiffness matrix and load vector for two noded beam element?
4. (a) Derive the shape functions for a Hexahedral element.
(b) Explain the various convergence requirements.
5. find the displacements and reaction forces for the Fig 3 given below. Assume $\mathrm{E}=$ $2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$.


Figure 3
6. A composite wall consists of 4 cm thick wood, 10 cm glass fiber insulation, and 1 cm thick plaster. If the temperature on wood and plaster faces are $20^{\circ} \mathrm{C}$ and
$-20^{\circ} \mathrm{C}$ respectively. Determine the temperature distribution in the wall. Assume the thermal conductivity of wood, glass fiber and plaster are $0.17,0.035$ and $0.5 \mathrm{~W} / \mathrm{m}$ K respectively and colder side heat transfer coefficient is $25 \mathrm{~W} / \mathrm{m}^{2} \mathrm{~K}$.
7. Determine the natural frequencies and mode shapes of a stepped bar as shown in figure 8 using the characteristic polynomial technique. Assume $\mathrm{E}=250 \mathrm{Gpa}$ and density is $7850 \mathrm{~kg} / \mathrm{m}^{3}$.


10 kN

Figure 8
8. The coordinates of the nodes 1,2 and 3 of a triangular element are ( 1,1 ), ( 8,4 ) and $(2,7) \mathrm{in} \mathrm{mm}$. The displacements at the nodes are $u_{1}=1 \mathrm{~mm}, u_{2}=3 \mathrm{~mm}, u_{3}$ $=-2 \mathrm{~mm}, \mathrm{v}_{1}=-4 \mathrm{~mm}, \mathrm{v}_{2}=2 \mathrm{~mm}$ and $\mathrm{v}_{3}=5 \mathrm{~mm}$. Obtain the strain-displacement relations, matrix B and detemine the strains $\varepsilon_{x}, \varepsilon_{y}$ and $\gamma_{x y}$.

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## Answer any FIVE Questions

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Figure 2
6. (a) Derive the shape functions for a Hexahedral element.
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Figure 3

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