IV B.Tech I Semester Examinations,November 2010 ADVANCED CONTROL SYSTEMS
Electrical And Electronics Engineering
Time: 3 hours
Answer any FIVE Questions
All Questions carry equal marks

1. (a) Explain Minimum - Time problem?
(b) Explain State Regulator problem in brief?
2. (a) Consider a linear system described by the differential equation $y+2 y+y=$ $\stackrel{\circ}{\mathrm{u}}+u$ Test for controllability and observability.
(b) Define and explain the concept of controllability
3. (a) Find U * for the system $\dot{x}=-\mathrm{x}+\mathrm{ux}(0)=1$ which minimizes

$$
J=\frac{1}{2} \int_{0}^{2}\left(x^{2}+u^{2}\right) d t
$$

(b) What is a Hamiltonian. Formulate the optimal control problem in terms of Hamiltonian.
4. (a) A single-input system is described by the following state equation.

$$
\dot{X}=\left[\begin{array}{ccc}
-1 & 0 & 0 \\
1 & -2 & 0 \\
0 & 1 & -3
\end{array}\right] x+\left[\begin{array}{c}
10 \\
1 \\
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\end{array}\right] u
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Design a state feedback controller which will give closed-loop poles at $1 \pm \mathrm{j} 2,-6$.
(b) Draw the block diagram and deduce the expression for transfer function for the controller-observer.
5. Obtain the Hamilton- Jacobi equation for the system
$\mathrm{X}_{1}=\mathrm{X}_{2}$
$\mathrm{X}_{2}=2 \mathrm{X}_{1}+4$
$\mathrm{J}=\mathrm{X}(0)=0$
To minimize
$\mathrm{J}=1 / 2 \mathrm{X}^{2}\left(\mathrm{t}_{1}\right) \int_{0}^{t_{1}} 1 / 2\left(x_{1}^{2}+x_{2}^{2}+u^{2}\right) d t$
Final $t_{1}$ is specified. $\mathrm{U}(\mathrm{t})$ and $\mathrm{X}(\mathrm{t})$ are not constrained.
6. Check the stability of the system described by
$\dot{x}_{1}=-\mathrm{x}_{1}+2 \mathrm{x}_{1}^{2} \mathrm{x}_{2}$
$\dot{\mathrm{x}}_{2}=-\mathrm{x}_{2}$
by using the variable gradient method.
7. The following equation is called the Van der Pol equation.
$\ddot{x}-(1-x) \dot{x}+x=0$
Determine the type of the singular point and Draw a phase - plane portrait.
8. (a) Explain the multivalued responses and jump phenomenon
(b) Determine the describing function for the nonlinear element described by $\mathrm{y}=x^{3}$
where $\mathrm{x}=$ input to the nonlinear element (sinusoidal signal) and $\mathrm{y}=$ output of the nonlinear element.


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