# II B. Tech II Semester Supplementary Examinations, April/May-2017 PROBABILITY AND STATISTICS <br> (Com. to CE, CHEM, PE) 

Time: 3 hours
Max. Marks: 80
Answer any FIVE Questions
All Questions carry Equal Marks

1. a) There are two boxes .In Box -I, 11 cards there numbered 1 to 11 and in Box -II, 5 cards numbered 1 to 5 .A box is chosen and a card is drawn .If the card shows an even number, then another card is drawn from the same box. If the card shows an odd number, then another card is drawn other box .Find the probability that (i) both are even (ii) both are odd (iii) if both are even it is from box -I
b) A, B, and C in order toss a coin. The first one to toss head wins the game. What are the probabilities of winning, assuming that the game may continue indefinitely.
2. a) The p.d.f of $f(x)=\left\{\begin{array}{ll}\frac{x}{k} & , 0 \leq x \leq 400 \\ \frac{800-x}{k} & , 400 \leq x \leq 800\end{array}\right.$,then find value of k and also, 'a' so that $\mathrm{P}(\mathrm{x}<\mathrm{a})=0.7$
b) Define (i) random variable (ii) continuous (iii) discrete random variables with examples
3. a) Derive the expression for mean and variance of Binomial distribution
b) Find the moment generating function of $f(X)= \begin{cases}1 & , 0<x<1 \\ 0, \text { otherwise }\end{cases}$
4. Samples of size 2 are taken from the population 3, 6.9, 15, 27 with replacement. Find a) The mean of the population b) The standard deviation of the population c) Mean of the sampling distribution of means $d$ ) The standard deviation of the sampling distribution of means
5. a) Explain i) level of significance ii) critical region iii) confidence limits
b) In a survey of water coolers produced by company A, it won found that 19 machines were defective in a random sample of 200 while for company B, 5 were defective out of 100 . At 0.05 level, is there a reason to believe that there is a significant difference in the performance of the coolers of the two brands A and $B$.
6. a) A die is thrown 264 times with the following results. Show that the die is
basied. ( $\chi_{0.05}^{2}=11.07$ for 5 d.f)

| No. appeared on the die | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 40 | 32 | 28 | 58 | 54 | 52 |

b) Five coins are tossed 320 times the number of heads observed is given below.

Examine whether the coin is unbased.

| No. of heads | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 15 | 45 | 85 | 95 | 60 | 20 |

7. a) Find the coefficient of correlation between X and Y .

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 12 | 11 | 13 | 15 | 14 | 17 | 16 | 19 | 18 |

b) The number of defects on 20 items are given below

Item No. 1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20
No. of defects:2, $, 4,1,0,8,0,1,2,0,6,0,2,1,0,3,2,1,0,2$
Devise a suitable control scheme for the future.
8. a) Explain (M/M/1):( $\infty /$ FCFS) Queueing model
b) Barber a takes 15 minutes to complete one hair cut. Customers arrive in his shop at an average rate of one every 30 minutes. Barber B takes 25 minutes to complete one hair cut and customers arrive at his shop at an average rate of one every 50 minutes. The arrival processes are poisson and the service times follow an exponential distribution. i) Where would you expect a bigger queue.
ii) Where would you require more time waiting included to complete a hair cut

