

Roll No.

Total No. of Pages : 02

Total No. of Questions : 08

M.Tech. (ME) (Sem.-2nd)**COMPUTATIONAL FLUID DYNAMICS**

Subject Code : MME-504

Paper ID : [E0429]

Time : 3 Hrs.

Max. Marks : 100

INSTRUCTION TO CANDIDATES :

1. Attempt any FIVE questions out of EIGHT questions.
2. Each question carry TWENTY marks.

1. a) What are different methods used for solving engineering problems? Write their relative merits and demerits. What are different steps involved in theoretical modelling of a physical problem?
b) What are different governing equations used for solving the fluid mechanics and heat transfer problems? Write these equations in Cartesian co-ordinates. Also write different boundary conditions used for solving these governing equations.
2. a) Describe Finite Difference Method, Finite Element Method and Finite Volume Method. For what type of problems these methods are most suitable?
b) Derive the finite difference expressions for a second order derivative with forward, backward and central difference approximations.
3. a) Distinguish between discretization and round-off errors. Compare them with suitable examples.
b) Describe briefly: Consistency, Convergence and stability of a numerical solution.
4. A large plate of thickness $L = 2$ cm with constant thermal conductivity $k = 0.5$ W/mK and uniform heat generation $q = 1000$ kW/m³. The opposite faces of the plate are maintained at uniform temperature of 100°C and 200°C. Assuming the dimensions in y and z directions to be

so large that temperature gradient is significant in x direction. Determine the steady state temperature distribution using Finite Volume Method (FVM) and compare the results with analytical solution.

5. Explain the following methods with suitable examples and demerits:
 - I) Explicit method
 - II) Implicit method
 - III) Semi-implicit method
6. a) What is the purpose of defining different control volumes in the finite control volume method? Show that central difference approximation is second order of accuracy.
b) Verify the following difference approximation at the point (i, j) . Assume $\Delta x = \Delta y = h$

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = \frac{T_{i+1,j-1} + T_{i+1,j+1} + T_{i-1,j-1} + T_{i-1,j+1} - 4T_{i,j}}{2h^2}$$

- a) Describe the SIMPLE pressure-correction method for solving coupled mass and momentum equations. Explain why, in practice, it is necessary to correct the velocity field to satisfy mass conservation.
- a) Show that the QUICK advection scheme is second order accurate on a uniform mesh).
- b) Discuss the various relaxation techniques used in iterative solution of linear algebraic equations.
- c) Describe the Tri-Diagonal Matrix Algorithm for solving linear algebraic equations.

