

**(DMCA108)**

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**M.C.A. DEGREE EXAMINATION, MAY- 2018****First Year****DISCRETE MATHEMATICS****Time :3 Hours      Maximum Marks :70****SECTION - A****Answer any three of the following questions.****(3 x 15 = 45)**

- Q1)** a) Prove that, for any three propositions  $p, q, r$ , the compound proposition  $[(p \rightarrow q) \wedge (q \rightarrow r)] \rightarrow (p \rightarrow r)$  is tautology.  
b) Obtain principle disjunctive normal form of the following.  
 $P \rightarrow \{(p \rightarrow q) \wedge \neg(\neg q \vee \neg q)\}$
- Q2)** a) Prove that  $f^{-1} \circ g^{-1} = (g \circ f)^{-1}$ , where  $f: Q \rightarrow Q$  such that  $f(x) = 2x$  and  $g: Q \rightarrow Q$  such that  $g(x) = x+2$  are two functions.  
b) On the set of integers, the relation  $R$  is defined by " $aRb$ " if and only if " $(a - b)$  is even integer". Show that  $R$  is an equivalence relation.
- Q3)** Solve the following recurrence relations:  
i)  $a_{n+1} - 2a_n = 2^n, n \geq 0, a_0 = 1$   
ii)  $a_n = 3a_{n-1} - 2a_{n-2}$  for  $n \geq 2$
- Q4)** a) A non-empty subset  $S$  of  $G$  is a sub group of  $(G, *)$  iff for any pair of elements  $a, b \in S$ .  
b) Let  $G$  be the set of all nonzero real numbers, for  $a*b = ab/2$ , show that  $(G, *)$  is Abelian group.
- Q5)** What is partial order and partial order set? Draw Hasse diagram for poset  $(P(A), \subset)$  where  $A = \{1, 2, 3, 4\}$  is the power set of  $A$ .

**SECTION - B****Answer any five of the following questions.****(5 x 4 = 20)**

- Q6)** Prove that the logical equivalence of  $[p \wedge (p \rightarrow q) \wedge r] \equiv [(p \vee q) \rightarrow r]$ .
- Q7)** Show that  $\forall x(P(x) \vee Q(x)) \equiv \forall xP(x) \wedge \forall xQ(x)$ .
- Q8)** In how many ways can 4 mathematics books, 3 history books, 3 chemistry books and 2 sociology books be arranged on the shelf so that all books of the same subject are together?

**Q9)** What are the reflexive, symmetric and transitive relations?

**Q10)** Let  $f(x) = x+2$ ,  $g(x) = x-2$ ,  $h(x) = 3x$  for  $x \in \mathbb{R}$  where  $\mathbb{R}$  is set of real numbers.  
Find  $\text{gof}$ ,  $\text{hof}$ .

**Q11)** Show that the semi group  $(\mathbb{Z}, +)$  and  $(E, -)$  where  $E$  is the set of even integers are isomorphic.

**Q12)** Solve the linear recurrence relation:  $a_0 = 4a_{n-1} + 5a_{n-2}$  with  $a_1 = 2$ ,  $a_2 = 6$ .

**Q13)** Let  $G$  be group and let  $a, b, c \in G$ , then show that:

- i)  $ab=bc \Rightarrow b=c$
- ii)  $(ab)^{-1} = b^{-1}a^{-1}$

### **SECTION - C**

**Answer all of the following questions. (5 x 1 = 5)**

**Q14)** Define monoid.

**Q15)** Define Lattice.

**Q16)** Define binary relation.

**Q17)** Define disjunctive normal form.

**Q18)** What is generating function.

