# GUJARAT TECHNOLOGICAL UNIVERSITY <br> MCA - SEMESTER - II • EXAMINATION - SUMMER 2018 

Subject Code: $\mathbf{6 2 0 0 0 5}$
Date: 23-May-2018

## Subject Name: Computer Oriented Numerical Methods

Time: $\mathbf{1 0 . 3 0}$ am to 1.00 pm Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) Find the root of the equation $x^{3}-x-4=0$ using the Bisection method.

Perform iterations until the accuracy till four significant digit.
(b) Find the root of the equation $\mathrm{x}^{4}+24 \mathrm{x}-50=0$ correct up to three significant digits using Birge-Vieta method. Assume the initial value of the root $=1.5$
Q. 2 (a) (i) Explain total numerical error. How can one control numerical errors ?
(ii) State Descartes rule of sign. Use it to determine the number of positive and negative roots of the polynomial equation : $x^{4}-3 x^{3}+2 x^{2}+20 x-20=0$
(b) Use secant method to find a root of the following equation $x^{3}-5 \mathrm{x}+3=0$, correct up to three decimal places.

OR
(b) Use Newton-Raphson method to find a root of the following
equation $x^{3}-4 \mathrm{x}-9=0$, correct up to three decimal places between 2.625 and 3 .
Q. 3 (a) From the following table, find $y$ when $x=0.4$ using Lagrange's interpolation
formula.

| X | 0.3 | 0.5 | 0.6 |
| :--- | :--- | :--- | :--- |
| y | 0.61 | 0.69 | 0.72 |

(b) Fit a straight line of the form $\mathrm{y}=\mathrm{a}+\mathrm{b} x$, to the following data :

| x | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 5.1 | 5.3 | 5.6 | 5.7 | 5.9 | 6.1 |

OR
Q. 3 (a) Compute value of y at $\mathrm{x}=0.02$ using suitable interpolating polynomial

| X | 0.0 | 0.1 | 0.2 | 0.3 | 0.4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 1.0000 | 1.1052 | 1.2214 | 1.3499 | 1.4918 |

(b) Fit an exponential curve for the following data:

| $x$ | 600 | 500 | 400 | 350 |
| :--- | :--- | :--- | :--- | :--- |
| $y$ | 2 | 10 | 26 | 61 |

Q. 4 (a) Compute the second order derivative for the following set of data values at $\mathbf{x}=\mathbf{3}$

| X | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~F}(\mathrm{x})$ | -5 | 1 | 9 | 25 |

(b) Evaluate $\int_{1}^{2} e^{\left(-\frac{1}{2} x\right)} d x$ using trapezoidal rule for four intervals.

## OR

Q. 4 (a) The distance $(s)$ covered by a car in a given time $(t)$ is given in the
following table :

| Time (minutes) | 10 | 12 | 16 | 17 | 22 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Distance $(\mathrm{kms})$ | 12 | 15 | 20 | 22 | 32 |

Find speed of the car at $\mathrm{t}=14$ minutes.

Evaluate $\int_{2}\left(x^{2}+2 x\right) d x$ www. FirstRanker.com $\begin{gathered}\text { using Gauss Quadrature formula. }\end{gathered}$
Q. 5 (a) Solve the following system of simultaneous linear equations using Gauss-

Elimination method:
$2 x+8 y+2 z=14$
$x+6 y-z=13$
$2 x-y+2 z=5$
(b) Given $d y / d x=1+y^{2}$ with $\mathrm{y}(0)=0, \mathrm{y}(0.2)=0.2027, \mathrm{y}(0.4)=0.4228, \mathrm{y}(0.6)=0.6841$.
compute $\mathrm{y}(0.8)$ using Milne simpson's Predictor-Corrector method.
OR
Q. 5 (a) Solve the following system of simultaneous linear equations using Gauss-

Seidel method:
$10 x+y+2 z=44$
$2 x+10 y+z=51$
$x+2 y+10 z=61$
(b) Given $d y / d x=1+y^{2}$ with $\mathrm{y}(0)=0, \mathrm{y}(0.2)=0.2027, \mathrm{y}(0.4)=0.4228, \mathrm{y}(0.6)=0.6841$.
compute $\mathrm{y}(0.8)$ using Adam-Bashforth Predictor-Corrector method.

