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# B.Tech I Year I Semester (R15) Supplementary Examinations June 2018

## **MATHEMATICS – I**

(Common to all branches)

Time: 3 hours

Max. Marks: 70

#### PART - A

(Compulsory Question)

- Answer the following:  $(10 \times 02 = 20 \text{ Marks})$ 
  - (a) Solve  $[\cos x \tan y + \cos(x+y)]dx + [\sin x \sec^2 y + \cos(x+y)]dy = 0.$
  - (b) Solve  $(x+1)\frac{dy}{dx} y = e^x(x+1)^2$ .
  - Find the particular integral of  $(D^2 + 4D + 4)y = \frac{e^{-2x}}{x^2}$ .
  - Solve  $(x^2D^2 xD + 1)y = 0$ .
  - Find the radius of curvature for the curve y = 4sinx sin2x at  $x = 90^{\circ}$ .
  - If  $u = \frac{y^2}{x}$ ,  $v = \frac{x^2}{y}$  find  $\frac{\partial(u,v)}{\partial(x,y)} = ?$ Evaluate  $\int_0^a \int_0^{\sqrt{ay}} xy \ dx \ dy$ . Evaluate  $\int_0^\pi \int_0^{a\cos\theta} r\sin\theta \ dr \ d\theta$ .
  - (g)
  - (h)
  - Find the unit vector normal to the surface  $x^2 y^2 + z = 2$  at the point (1, -1, 2). (i)
  - Show that  $\vec{F} = (y^2 + 2xz^2)\vec{t} + (2xy z)\vec{j} + (2x^2z y + 2z)\vec{k}$  is irrotational. (j)

#### PART - B

(Answer all five units, 5 X 10 = 50 Marks)

- (a) Solve  $\frac{d^2y}{dx^2} 5\frac{dy}{dx} + 6y = x^2 + 3$ .
  - (b) Prove that the system of confocal and coaxial parabolas  $y^2 = 4a(x + a)$  is self orthogonal.

- (a) Solve  $(D^2 + 4D + 3)y = e^x sinx$ . (b) Solve  $\frac{dy}{dx} + \frac{x}{1-x^2}y = x\sqrt{y}$ .

Solve  $\frac{d^2y}{dx^2} + y = cosee x$  by using method of variation of parameters. 4

Solve  $(x+2)^2 \frac{d^2y}{dx^2} - (x+2)\frac{dy}{dx} + y = 3x + 4$ . 5

- 6 Expand  $\sin(xy)$  in powers of (x-1) and  $(y-\pi/2)$  upto second degree terms.
  - Discuss the maximum and minimum of  $f(x,y) = x^3 + y^3 12x 3y + 20$ .

- If  $x = rsin\theta \cos\theta$ ,  $y = rsin\theta \sin\phi$  and  $z = rcos\theta$  find  $\frac{\partial(x,y,z)}{\partial(r,\theta,\phi)}$ . 7
  - Show that the rectangular solid of maximum volume that can be inscribed in a sphere is a cube.

UNIT - IV

- Evaluate  $\iint_R (x^2 + y^2) dx dy$ , where R is the square  $0 \le x \le a$ ,  $0 \le y \le a$ . 8 (a)
  - Transform the integral into polar-co-ordinates and hence evaluate  $\int_0^a \int_0^{\sqrt{a^2-x^2}} \sqrt{x^2+y^2} \, dy \, dx$ . (b)

- (a) Change the order of integration in  $\int_0^a \int_x^a (x^2 + y^2) dy dx$  and then evaluate.
  - Find the area included between the curves  $y^2 = 4x$  and  $x^2 = 4y$ .

- If  $\vec{F} = (3x^2 + 6y)\vec{i} 14yz\vec{j} + 20xz^2\vec{k}$ , evaluate  $\int_{\mathcal{C}} \vec{F} \cdot \vec{dr}$  where C is the straight line joining (0,0,0) to 10
  - Using Stokes theorem, evaluate  $\int_{C} \vec{F} \cdot \vec{dr}$  for the function  $\vec{F} = x^{2} \vec{i} + xy \vec{j}$  in XOY-plane bounded by x = 0, y = 0, x = a, y = a.

Verify Divergence theorem for  $\vec{F} = (x^2 - yz)\vec{i} + (y^2 - zx)\vec{j} + (z^2 - xy)\vec{k}$  taken over the rectangular 11 parallelepiped x = 0, x = 1, y = 0www.xirstRanker.xom