

Code No: 113AN

R13**JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD****B.Tech II Year I Semester Examinations, November - 2015****PROBABILITY AND STATISTICS****(Common to ME, CSE, IT, MCT, AME, MIE, MSNT)****Time: 3 Hours****Max. Marks: 75****Note:** This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit.

Each question carries 10 marks and may have a, b, c as sub questions.

PART- A**(25 Marks)**

- 1.a) Explain, with suitable examples, discrete and continuous random variables. [2M]
- b) Find the first 3 moments about origin from Moment generating function of the Binomial distribution. [3M]
- c) Write the relation between correlation and regression coefficients. Is it possible to have two variables x and y with regression coefficient as 2.8 and -0.5? Explain. [2M]
- d) Is the function $f(x) = \begin{cases} \frac{1}{2}x e^{-y}, & 0 < x < 2, y > 0 \\ 0, & \text{Otherwise} \end{cases}$ can be considered as a joint density function of two random variables X and Y ? [3M]
- e) Write the standard error of (i) sample mean (ii) difference of two sample means. [2M]
- f) Mean of population = 0.700, mean of the sample = 0.742, standard deviation of the Sample = 0.040 sample size = 10. Test the null hypothesis for population mean = 0.700. [3M]
- g) Explain queue classification-Kendall's notation. [2M]
- h) Write:
- i) the relation between Expected number of customers in the queue and in the system.
 - ii) waiting time of a customer in the queue and in the system
 - iii) the formula for finding the probability that there are more than n customers in the system. [3M]
- i) Classify the random processes. [2M]
- j) Find the values of x, y, z in order for $\begin{bmatrix} 0 & x & 1/3 \\ 0 & 0 & y \\ 1/3 & 1/4 & z \end{bmatrix}$ to be transition matrix. [3M]

PART-B
(50 Marks)

- 2.a) Is $f(x) = \frac{1}{2}x^2e^{-x}$ when $x \geq 0$ can be regarded as a probability function for a continuous random variable? If, so find Mean and Variance of the random variable.
- b) Find the moment generating function of the Normal distribution. Show that all odd order moments of a normal distribution are zero. [5+5]

OR

- 3.a) In a sample of 1000 cases, the mean of a certain test is 14 and standard deviation is 2.5. Assuming the distribution to be normal, find:
- How many students score between 12 and 15?
 - How many score above 18?
 - How many score below 18?
- b) Find the Moment generating function of Poisson distribution and find the first 3 moments. [5+5]

- 4.a) If X and Y are two random variables having joint density function

$$f(x, y) = \begin{cases} \frac{1}{8}(6-x-y), & 0 \leq x \leq 2, 2 \leq y < 4 \\ 0, & \text{otherwise} \end{cases}$$

Find: i) $P(X < 1/Y < 3)$ ii) $f_X(x)$ & $f_Y(y)$.

- b) Find the coefficient of correlation between X and Y for the following data. [5+5]

X	1	2	3	4	5	6	7	8	9
Y	10	11	12	14	13	15	16	17	18

OR

- 5.a) Joint distribution of X and Y is given by $f(x, y) = 4xy e^{-(x^2+y^2)}$; $x \geq 0, y \geq 0$. Test whether X and Y are independent. Also find conditional density of X given $Y=y$.
- b) For the following data, find equations of the two regression lines. [5+5]

X	1	2	3	4	5
Y	15	25	35	45	55

- 6.a) Fit a binomial distribution to the following data and test the goodness of fit.

x	0	1	2	3	4
f	38	144	342	287	164

- b) A researcher wants to know the intelligence of students in a school. He selected two groups of students. In the first group there 150 students having mean IQ of 75 with a S.D of 15 in the second group there are 250 students having mean IQ of 70 with S.D of 20. Is there a significant difference between the means of two groups? [5+5]

OR

- 7.a) Fit a Poisson distribution to the following data and test the goodness of fit.

x	0	1	2	3	4	5	6
Observed frequency	275	72	30	7	5	2	1

- b) In a city A 20% of a random sample of 900 school boys had a certain physical defect. In another city B 18.5% of a random sample of 1600 school boys had the same defect. Is the difference between the proportions significant? [5+5]
- 8.a) State and prove Arrival Distribution theorem.
- b) In a telephone exchange the arrival of calls follow Poisson distribution with an average of 8 minutes between two consecutive calls. The length of a call in 4 minutes. Determine:
- The probability that the person arriving at the booth will have to wait
 - The average queue length that forms from time to time. [5+5]

OR

- 9.a) Prove that the probability of having 'n' customers in the queuing system (M/M/1) : (∞ , FCFS) is $P_n = \rho^n (1 - \rho)$, where ρ is traffic intensity of the system
- b) In a public Telephone both the arrivals are on the average 15 per hour. A call on the average takes 3 minutes. If there is just one phone, find (i) expected number of callers in the booth at any time (ii) The proportion of the time the booth is expected to be idle. [5+5]

- 10.a) Write about the different states of the Stochastic process.
- b) The three state markov chain is given by the transition probability matrix

$$P = \begin{pmatrix} 0 & 2/3 & 1/3 \\ 1/2 & 0 & 1/2 \\ 1/2 & 1/2 & 0 \end{pmatrix}. \text{ Prove that the chain is irreducible. [5+5]}$$

OR

- 11.a) The transition probability matrix of a Markov chain $\{X_n\}; n=1,2,3 \dots$ having

three states 1,2,3 is $\begin{bmatrix} 0.1 & 0.5 & 0.4 \\ 0.6 & 0.2 & 0.2 \\ 0.3 & 0.4 & 0.3 \end{bmatrix}$ and the initial distribution is

$$P^{(0)} = \{0.7, 0.2, 0.1\} \text{ then find } P = \{X_3 = 2, X_2 = 3, X_1 = 3, X_0 = 2\}$$

- b) The transition probability matrix of a Markov chain is given by $\begin{bmatrix} 0.3 & 0.7 & 0 \\ 0.1 & 0.4 & 0.5 \\ 0 & 0.2 & 0.8 \end{bmatrix}$.
- Is this Matrix irreducible? [5+5]

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