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	Code No: 131AB	
	JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD B. Tech I Year I Semester Examinations, December - 2016	***
	MATHEMATICS-II (Common to CE, ME, MCT, MMT, MIE, CEE, MSNT)	
	Time: 3 hours Max. Marks: 75	
	Nöte: This question paper contains two:parts A and B.:: Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions.	× × × × × × × × × × × × × × × × × × ×
··.	PART- A: (25 Marks)	ļ
	1.a) Find the Laplace transform of the function $f(t) = \begin{cases} t & 0 < t < a \\ -t + 2a & a < t < 2a \end{cases}$ [2]	
ii j	b) Prove that $L^{-1}\{F(s)\} = f(t)$ and $f(0) = 0$ then $L^{-1}\{sF(s)\} = \frac{df}{dt}$. [3] c) Evaluate $\int_0^\infty a^{-\frac{t}{2}} dx$. [3] d) Show that $\beta(p,q) = \beta(p+1,q) + \beta(p,q+1)$. [3] e) Find the area bounded by the curves $y = x, y = x^2$. [2]	
	 f) Evaluate \$\int_0^a \int_0^{\sqrt{a^2-y^2}}(x^2 + y^2) \ dy dx\$ by changing into polar coordinates. [3] g) Find the directional derivative of \$xyz^2 + xz\$ at \$(1,1,1)\$ in a direction of the normal to the surface \$3xy^2 + y = z\$ at \$(0,1,1)\$;: [2] h) Find a unit normal vector to the surface \$x^2 + y^2 + 2z^2 = 26\$ at the point \$(2,2,3)\$. [3] i) Find the work done by the force \$\vec{F} = 3x^2i + (2xz - y)j + zk\$ along the straight line joining the points \$(0,0,1)\$ and \$(2,1,3)\$. 	
	j) Find the circulation of \vec{F} round the curve c where $\vec{F} = (e^x \sin y)i + (e^x \cos y)j$ and c is the rectangle whose vertices are $(0,0), (1,0), (1,\frac{\pi}{2}), (0,\frac{\pi}{2})$.	V. 3.
	PART-B	
	(50 Marks)	
	2. Solve the differential equation $\frac{d^2x}{dt^2} - 4\frac{dx}{dt} - 12x = e^{3t}$ given that $x(0) = 1$ and $x'(0) = -2$ using Laplace transforms. [10]	
	OR 3. Use Laplace transforms, solve $y(t) = 1 - e^{-t} + \int_0^t y(t-u) \sin u du$.	, , , ,
	4.a) Prove that $\Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$. b) Prove that $\Gamma(n)\Gamma(1-n) = \frac{\pi}{\sin n\pi}$. [5+5]	
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₩ . 4 h e w		•				$(x^2)^n dx$ where <i>n</i> is	a
	b) If n	n and n are positiv	ve integers then p	rove that $B(m, n)$	$(n) = \frac{(m-1)(n-1)!}{(m+n-1)!}.$	[5+5]	
	6. The	plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{a}$ hedron $OABC$. A	$\frac{z}{z} = 1$ meets the also find its mass	axes in A, B if the density at	and C. Find t	he volume of th	le
·		nge the order of i				•	
		luate ∭ <i>xyzdxd</i>		0 2 / 4		$a^2 + a^2 = a^2$	
	<i>5)</i> E (a	iaace jij <i>nyzan</i> a	yaz över me pos	invo ociani or ii	ie sphere x + y	[5+5]	
* * * * * * * * * * * * * * * * * * *		I the directional dace $3xy^2 + y = 2$		$x^2 + xz$ at (1,1,1)) in a direction o	of the normal to the	e
		we that curl $(\vec{a} \times \vec{b})$		$\operatorname{div} \vec{a} + (\vec{b} \cdot \nabla)\vec{c}$	$\vec{n} = (\vec{a} \cdot \nabla) \vec{h}$	[5+5]	
	. 0) 110	re that carr (a × z		OR	(u v)0	[515]	
*	9Prov	we that if \vec{r} is the modial if $\vec{n} = -3$.	position vector o	f any point in s	pace then $r^n \vec{r}$ is	irrotational and is [10]	\$
	10. Veri of th	fy divergence the e cylinder $y^2 + z$	orem for $2x^2yi - x^2 = 9$ and $x = 2$	$-y^2j + 4xz^2k t$	aken over the reg	gion of first octant [10]	
	$ \begin{array}{ccc} 1 & & \text{If } \vec{f} \\ & & \text{integ} \end{array} $	$= 3x^2 \ddot{y} \ddot{z}^2 \ddot{i} + x^2$ ration. Hence eva	$z^2j + 2x^3yzk$. Solution in Solution in Section 2.	how that $\int_C \vec{f}$ when C is any	$d\vec{r}$ is findependent path joining (0, 0)	ent of the path of (1, 2, 3). [10]	
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