Subject Code: R13102/R13 | Set No - 1 |

I B. Tech I Semester Regular Examinations Jan./Feb. - 2015
MATHEMATICS-I
(Common to All Branches)

Time: 3 hours   **Max. Marks: 70**

Question Paper Consists of **Part-A** and **Part-B**
Answering the question in **Part-A** is Compulsory,
Three Questions should be answered from **Part-B**
*****

PART-A

1.(i)   solve the D.E $(1+xy)x\, dy +(1-yx)y\, dx = 0$

(ii)   Solve $(D^2+4)\, y = \sin 2x$

(iii) Expand $e^x \cos y$ near $(1, \pi/4)$ by Taylors series method

(iv)   Find $L\left(\int_0^t e^{-t} \cos t\, dt\right)$

(v)   Solve $z(y-x) = qy^2 - px^2$ where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

(vi)   Solve by method of separation of variables $2x\dfrac{\partial z}{\partial x} - 3y\dfrac{\partial z}{\partial y} = 0$

[4+3+4+4+4+3]

PART –B

2.(a) Find the equation of the curve satisfying the D.E $\left(1+x^2\right)dy + (2xy - 4x^2)dx = 0$ and passing through origin

(b)   Find the equation of the system of orthogonal trajectories of the family of the curves $r^n \sin n\theta = a^n$, where 'a' is a parameter.

[8+8]

3.(a) solve the D.E $D^2\left(D^2+4\right) y = 320(x^3 + 2x^2 + e^x)$

(b)   Solve the D.E $y^{111} + y = \cos(2x-1)$

[8+8]

4.(a) Find the maximum and minimum values of $x^3 - 3xy^2 - 15x^2 - 15y^2 + 72x$

(b)   If $z = \log(e^x + e^y)$ *show that* $\left(\dfrac{\partial^2 z}{\partial x^2}\right)\left(\dfrac{\partial^2 z}{\partial y^2}\right) = \dfrac{\partial^2 z}{\partial x\partial y}$

[8+8]

5.(a) Solve the D.E $\left(D^2 + 2D + 1\right) = 3te^t$ *if* $y(0) = 4\, \&\, y^1(0) = 2$ using Laplace transform

(b)   Using Convolution theorem find $L^{-1}\left(\dfrac{1}{s^2(1+s)^2}\right)$

[8+8]

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$\boxed{\textbf{Set No - 1}}$

6.(a)   Solve the P.D.E $p/x^2 + q/y^2 = z$, where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

   (b)   Obtain P.D.E of all spheres whose centre lies on z – axis with a given radius r.

[8+8]

7.   An insulated rod of length L has its ends A and B maintained at 0^0c and 100^0c respectively under steady state conditions prevail .If B is suddenly reduced to 0^0c and maintained at 0^0c ,find the temperature at a distance x from A at time t

[16]

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PART-A

1.(i)   Solve the D.E $y(2x^2 y + e^x)dx = (y^3 + e^x)dy$

  (ii)   Write the Equation of simple harmonic motion and find its solution

  (iii)   Find the relation between the functions $u = \dfrac{x}{y}$ & $v = \dfrac{x+y}{x-y}$

  (iv)   Find $L\left(\dfrac{e^{-at} - e^{-bt}}{t}\right)$

  (v)   Solve the P.D.E $xp - yq = y^2 - x^2$ where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

  (vi)   Solve the $(D^2 - 2DD')z = e^{2x} + x^3 y$ where $D = \dfrac{\partial}{\partial x}, D^1 = \dfrac{\partial}{\partial y}$

                                                        [4+3+4+4+4+3]
PART –B

2.(a)   A radioactive substance disintegrates at a rate proportional to it's mass. When it's mass is
         10 mgm, the rate of disintegration is 0.051 mgm per day. How long will it take for the
         mass to be reduced from 10 mgm to 5 mgm.

  (b)   Solve $\dfrac{dy}{dx} = x^3 - 2xy$ *if* $y(1) = 2$.

                                                        [8+8]
3.(a)   solve the D.E $(D^2 - 1) y = x \sin x$

  (b)   Solve the D.E $y^{111} - y^{11} - y^1 + y = 1 + x^2$

                                                        [8+8]
4.(a)   if u = f(r) and x = rcosθ, y = rsinθ then prove that $\left(\dfrac{\partial^2 u}{\partial x^2}\right) + \left(\dfrac{\partial^2 u}{\partial y^2}\right) = f^{11}(r) + \dfrac{1}{r} f^1(r)$

  (b)   If the sum of three numbers is a constant, then prove that their product is maximum when
         they are equal.

                                                        [8+8]

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$\boxed{\textbf{Set No - 2}}$

5.(a) Find $L^{-1}\left(\dfrac{s+1}{s^2(1+s)^2}\right)$

  (b) Using Laplace transform, Evaluate $\displaystyle\int_0^\infty \dfrac{e^{-at}\sin^2 t}{t}dt$

  [8+8]

6.(a) Form the partial Differential equation by elimination $F(xy+z^2, x+y+z)=0$

  (b) Solve the P.D.E $z(z^2+xy)(px-qy)=x^4$ where $p=\dfrac{\partial}{\partial x}, q=\dfrac{\partial}{\partial y}$

  [8+8]

7. A string of length 100 cm is tightly stretched between x = 0 and x = 100 and is displaced from its equilibrium positions by imparting each of its points an initial velocity given by

$$g(x)=\begin{cases} x & if & 0\le x\le 50 \\ 100-x & if & 50<x\le 100 \end{cases}$$

Then find the displacement at any subsequent time.

  [16]

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Set No - 3

I B. Tech I Semester Regular Examinations Jan./Feb. - 2015
MATHEMATICS-I
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*****

PART-A

1.(i)   Solve the D.E $y^2 dx + \left(-y^2 + x^2 - xy\right) dy = 0$

(ii)   Solve the D.E $(D^4 + 18D^2 + 81)y = 0$

(iii) If x = r cosθ , y = r sinθ then prove that $\dfrac{\partial r}{\partial x} = \dfrac{\partial x}{\partial r}$ & $\dfrac{1}{r}\dfrac{\partial x}{\partial \theta} = r\dfrac{\partial \theta}{\partial x}$

(iv)   Find $L^{-1}\left\{\log\left(1+\dfrac{1}{s^2}\right)\right\}$

(v)   Solve the P.D.E $p(1+q) = qz$ where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

(vi)   Solve $\left(D^3 - 3D^2 D' + 4D'^2\right) = e^{x+2y}$ where $D = \dfrac{\partial}{\partial x}, D^1 = \dfrac{\partial}{\partial y}$

[4+3+4+4+4+3]

PART –B

2.(a) If the air temperature is 20^0c and the body cools for 20 min from 140^0c to 80^0c , find when the temperature will be 35^0c.

(b)   Solve the D.E $dr + \left(2r \cot\theta + \sin 2\theta\right) d\theta = 0$

[8+8]

3.(a) Solve the D.E $\left(D^2 + 2D + 1\right) y = xe^x \cos x$

(b)   Solve the D.E $y^{11} - 2y^1 + y = 1 + e^x$

[8+8]

4.(a) Find the dimensions of the rectangular box open at the top of the maximum capacity whose surface area is 108 sq.inches.

(b)   Show that $\log(1+e^x) = \log 2 + \dfrac{x}{2} + \dfrac{x^2}{8} - \dfrac{x^4}{48} + ...$ and

Hence deduce that $\dfrac{e^x}{1+e^x} = \dfrac{1}{2} + \dfrac{x}{4} - \dfrac{x^3}{48} + ..$

[8+8]

5.(a) Find the Laplace transform of Dirac-Delta function

(b)   Solve the D.E $y^{111} + y = 1\, if\, y(0) = y^1(0) = y^{11}(0) = 0$ using Laplace transform

[8+8]

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$\boxed{\textbf{Set No - 3}}$

6.(a) Solve the P.D.E p cos (x +y) + q sin (x + y) = z where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

  (b) Obtain P.D.E by eliminating arbitrary functions from z = f (2x+3y) + g (3x-y)

[8+8]

7.   A square plate is bounded by the lines x =0, y=0, x =*l*, y =*l*. Its faces are insulated .The temperature of along the upper horizontal edge is given by u (x. *l*) = x (*l*-x) when 0 < x< *l* while other edges are kept at zero. Find the steady state temperature.

[16]

Subject Code: R13102/R13 | Set No - 4 |

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MATHEMATICS-I
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Three Questions should be answered from **Part-B**
*****

PART-A

1.(i)   Solve the D.E $xy\,dx - (x^2 + 2y^2)dy = 0$

(ii) Find the particular integral of $(D^2 + 1) = \sec x$

(iii) If $u = \dfrac{y}{z} + \dfrac{z}{x}$ *then* *find* $x\dfrac{\partial u}{\partial x} + y\dfrac{\partial u}{\partial y} + z\dfrac{\partial u}{\partial z}$

(iv) Find $L\left[t^2 e^{-2t}\right]$

(v) Solve $z^2 = 1 + p^2 + q^2$ where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

(vi) Solve by method of separation of variables $4\dfrac{\partial z}{\partial x} + \dfrac{\partial z}{\partial y} = 3z$ *if* $u(0, y) = 3e^{-y} - e^{-5y}$

[4+3+3+4+4+4]

PART –B

2.(a) In a certain chemical reaction the rate of change of conversion of a substance at time t is proportional to the quantity of the substance still untransformed at that time. At the end of one hour 60 grams remain and at the end of four hours 21 grams. How many grams of the first substance was there initially.

(b) Find the orthogonal trajectories of the family of hypocycloids $x^{2/3} + y^{2/3} = a^{2/3}$, where 'a' is a parameter.

[8+8]

3.(a) Solve the D.E $\left(D^4 - 1\right) y = e^x \cos x$

(b) Solve the D.E $y^{111} - 2y^{1} + 2y = 1 + xe^x$

[8+8]

4.(a) Find the maximum value of $u = x^2 y^3 z^4$ *if* $2x + 3y + 4z = a$ by Lagrange's multiplier method.

(b) If x = u(1-v) and y = uv prove that $\dfrac{\partial(u,v)}{\partial(x,y)} \times \dfrac{\partial(x,y)}{\partial(u,v)} = 1$

[8+8]

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5.(a)   Solve the D.E $\left(D^2 + 6D + 9\right) = \sin t$ if $y(0) = 1$ & $y^1(0) = 0$ using Laplace transform

(b)   Find the $L\left(\dfrac{1 - \cos t}{t^2}\right)$

[8+8]

6.(a)   Solve the P.D.E pqz = p²(qx+p²)+ q²(py+q²) where $p = \dfrac{\partial}{\partial x}, q = \dfrac{\partial}{\partial y}$

(b)   Obtain P.D.E by eliminating arbitrary constants   a and b from $z = xy + y\sqrt{x + a} + b$

[8+8]

7.(a)   Solve $\left(D^2 - D'^2 - 3D + 3D'\right) z = xy + e^{x+2y}$, where $D = \dfrac{\partial}{\partial x}, D^1 = \dfrac{\partial}{\partial y}$

(b)   Find the physically feasible solution of one -dimensional heat flow equation.

[8+8]