

Code No: **R42022**

R10

Set No. 1

IV B.Tech II Semester Regular/Supplementary Examinations, April – 2015

ADVANCED CONTROL SYSTEMS

(Electrical and Electronics Engineering)

Time: 3 hours
Max. Marks: 75
Answer any FIVE Questions
All Questions carry equal marks

- 1 A unity feedback system is characterized by the closed loop transfer function

$$T(s) = \frac{s^2 + 4s + 3}{s^3 + 3s^2 + 2s + 4}$$

Construct the suitable signal flow graph and therefrom construct a state model of the system [15]

- 2 The state model of a linear time invariant system is given by

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 0 & -2 \\ 1 & 0 & -5 \\ 0 & 1 & -9 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} u$$

Determine the canonical form of the state model. [15]

- 3 a) Explain the principle of duality between controllability and observability. [8]

- b) Develop the matrix representation of MIMO system. [7]

- 4 a) Obtain the expression for describing functions with diagram [6]

- b) A nonlinear element system, with describing function, $K_N = (1/X) < -60^\circ$ in cascade with, $G(j\omega) = \frac{5}{j\omega(2 + j0.4\omega)}$. Find the limit cycle of the system. [9]

- 5 a) Explain the stability in the sense of Lyapunov. [6]

- b) A non-linear system described by the following equations

$$\dot{x}_1 = -x_1 + 2x_2$$

$$\dot{x}_2 = 3x_1 - x_2 - x_2^3$$

Observe the stability of equilibrium state. [9]

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- 6 State equation of linear time invariant is defined by $\dot{x} = Ax + Bu$

$$\text{where } A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -6 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$$

By using the state –feedback control $u = -Kx$, consider closed –loop poles at $s = -1 \pm j3$, $s = -7$. Calculate the state –feedback gain matrix K . [15]

- 7 Derive the Euler Lagrange equation and the boundary conclusion for the final time t_1 free and $x(t_1)$ specified, starting from a given $x(t_0)$ extremize

$$J(x) = \int_1^{t_1} g(x, \dot{x}, t) dt \quad [15]$$

- 8 Explain the linear quadratic optimal regular problem formulation. [15]

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Set No. 2

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Answer any FIVE Questions

All Questions carry equal marks

- 1 a) A linear time invariant system is characterized by the homogeneous state equation

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Determine the solution of homogeneous equation, assuming the initial state

vector $x_0 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$

[6]

- b) Consider now that the system has a forcing function and is represented by the

following non-homogeneous state equation $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u,$

Where u is a unit step function

Determine the solution of this equation, considering initial conditions of part(a)

[9]

- 2 The state model of a linear time invariant system is given by

$$\begin{bmatrix} \dot{x} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ -2 & -3 & 0 \\ 0 & 2 & -3 \end{bmatrix} \begin{bmatrix} x \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} u \end{bmatrix}$$

$$y = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \end{bmatrix}$$

Convert this state model to controllable phase variable form.

[15]

- 3 Explain the multi variable Nyquist plot and singular values analysis.

[15]

- 4 a) Discuss the basic concept of describing function methods.

[6]

- b) Explain the classification of non-linearities and give the examples for each.

[9]

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5 a) What are the sufficient conditions of Lyapunov stability [5]

b) Test the stability of the system described by

$$\dot{x}_1 = -2x_1 + 5x_1^2x_2$$

$$\dot{x}_2 = -3x_2$$

Determine the region of asymptotic stability using Krasovskii method [10]

6 a) Derive the Ackermann's formula for the determination of the state feedback gain matrix. [8]

b) Explain the effect of state feedback on controllability and observability. [7]

7 Calculate the extremal for the functional given below.

$$J(x) = \int_0^{t_1} (3x + 7\dot{x}^2) dt$$

$x(0) = 5, x(t_1) = 5, t_1 > 1$ [15]

8 Describe the optimal regulator design by parameter adjustment. [15]

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Answer any FIVE Questions
All Questions carry equal marks

- 1 The state model of a linear time invariant system is given by

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ -2 & -3 & -6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} u$$

Transform this state model into a canonical state model and there from obtain the explicit solution for the state vector and output when the control force 'u' is a unit step function and initial state vector is $X_0^T = [0 \ 1 \ 0]$

[15]

- 2 The state model of a linear time invariant system is given by

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ -1 & -2 & -1 \\ 0 & 0 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \\ 1 \end{bmatrix} u$$
$$y = [0 \ 1 \ -2] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

Determine the canonical form of the state model.

[15]

- 3 a) Explain controllability and observability form other canonical forms.

[8]

- b) Discuss the multi variable Nyquist plot.

[7]

- 4 Explain the following describing function with diagrams.

i) saturation non-linearity

ii) dead-zone non-linearity

[15]

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- 5 a) State and prove lyapunov stability theorem [7]
- b) Test the stability of the following system by using variable gradient method
 $\dot{x}_1 = -2x_1 + 3x_1^2x_2$
 $\dot{x}_2 = -4x_2$ [8]
- 6 The state equation of linear time invariant systems is

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ -1 & -2 & 1 \\ 3 & 0 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} -1 \\ 2 \\ 1 \end{bmatrix} u$$
 Consider the closed loop poles at $-1.5 \pm j4, -5.5$, design a state feedback controller. [15]
- 7 Consider the following system
 $\dot{x} = u$, with $|u| \leq 1$, determine the control which drive the system from an arbitrary initial state to the origin and minimize $J = \int_0^{t_1} |u(t)| dt$, t_1 is free. [15]
- 8 Explain the optimal regulator design by continuous time algebraic riccati equation. [15]

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Set No. 4

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Answer any FIVE Questions
All Questions carry equal marks

- 1 For the state model equation $\dot{x} = Ax$

Where $A = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 2 \\ -1 & -4 & -3 \end{bmatrix}$. Determine the initial condition vector $x_{(0)}$ which

will exist only the mode corresponding to the eigen value with the most negative real part

[15]

- 2 Test the observability of the systems for the following linear time invariant system using canonical form.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 2 & -1 & 3 \\ 1 & -1 & 1 \\ 1 & 2 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 3 \\ 1 \\ 5 \end{bmatrix} u$$

$$y = \begin{bmatrix} -2 & 1 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

[15]

- 3 a) Explain the controllability form Jordan canonical form. [7]
 b) Develop the transfer function representation of MIMO system. [8]
- 4 a) List out the common physical non-linearities with an example. [6]
 b) Describe the saturation and backlash non-linearities with neat diagram. [9]
- 5 a) State and explain Lyapunov stability analysis of control system. [7]
 b) Check the positive definite for given quadratic form as follows: [8]
 $Q = x_1^2 + 4x_2^2 + x_3^2 + 2x_1x_2 - 6x_2x_3 - 2x_1x_3$

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- 6 The closed loop transfer function of a plant

$$\frac{C(s)}{U(s)} = \frac{7}{s^3 + 2s^2 + 5s + 9}$$

With the help of state feedback control $u = -kx$, It is desired to place the closed loop poles at $-1 \pm j3.5$ and -4 . Calculate the necessary state feedback gain matrix 'K'. [15]

- 7 a) Explain the minimization of functionals of single input. [7]

- b) Calculate the curve with minimum arc length between the point $x(0) = 1.5$ and the line $t_1 = 3$. [8]

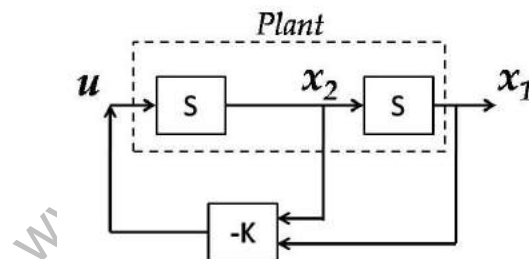
- 8 Consider the system shown in below figure. Assume the control signal to be

$$u(t) = -\bar{K}x(t)$$

Determine the optimal feedback gain matrix 'K' such that the following performance index is minimized.

$$J = \int_0^{\infty} (x^T Q x + u^2) dt$$

$$\text{Where, } Q = \begin{bmatrix} 1 & 0 \\ 0 & u \end{bmatrix}, (u \geq 0)$$



[15]