

Subject Code: R13107/R13
Set No - 1
I B. Tech I Semester Supplementary Examinations December - 2016
MATHEMATICS-II (MATHEMATICAL METHODS)

(Common to ECE, EEE, EIE, BioTech, EComE, Agri.E)

Time: 3 hours
Max. Marks: 70

Question Paper Consists of **Part-A** and **Part-B**
 Answering the question in **Part-A** is Compulsory,
 Three Questions should be answered from **Part-B**

PART-A

1. (a) Find the Root of the equation $3x = 1 + \cos x$ by using Iteration method.
- (b) If the interval of differencing is unity prove that $\Delta \left(\frac{2^x}{x!} \right) = \frac{2^x (1-x)}{(x+1)!}$
- (c) Find $y(1.1)$ by second order RK method given that $\frac{dy}{dx} = x - y$, $y(1) = 1$
- (d) Write the Fourier half range sine series for $f(x) = x$ in $[0, 1]$
- (e) Find $Z \left[\sin \frac{n\pi}{2} \right]$
- (f) If $F(p)$ is the complex Fourier transform of $f(x)$, then prove that complex Fourier transform of $f(x) \cos ax$ is $\frac{1}{2} [F(p+a) + F(p-a)]$

[3+3+4+4+4+4]

PART-B

2. (a) Find the root of the equation $4 \sin x = e^x$ by using bisection method.
 - (b) Find the root of the equation $x = x^4 - 10$ by using False position method.
- [8+8]
3. (a) Find the Lagrange's polynomial for the following data, hence find $y(15)$

x	-5	6	9	11
y	12	13	14	16

- (b) Fit a cubic polynomial for the following data
 $y_0 = -5, y_1 = -1, y_2 = 9, y_3 = 25, y_4 = 55, y_5 = 105$

[8+8]

4. (a) Evaluate $y(0.1)$, $y(0.2)$ by Taylor's series method for $\frac{dy}{dx} = \frac{x+y}{y-x}$, $y(0) = 1$.

- (b) By modified Euler's formula find $y(0.3)$, $y(0.6)$ given that $\frac{dy}{dx} = x^2 - y^2$, $y(0) = 1$

[8+8]

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 5. (a) Expand the function $f(x) = x^2$ as a Fourier series in $[\pi, \pi]$

 Hence deduce that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$

 (b) Find the Half range cosine series for $f(x) = x - x^2$ in $[0, 1]$

[8+8]

 6. (a) Using Fourier integral show that $e^{-ax} - e^{-bx} = \frac{2(b^2 - a^2)}{\pi} \int_0^\infty \frac{\lambda \sin \lambda x}{(\lambda^2 + a^2)} d\lambda, a, b > 0$

 (b) Find finite Fourier cosine transform of $f(x) = x + a$ for $0 < x < \pi$.

[8+8]

 7. (a) If $f(z) = \frac{2z + 3z + 4}{(z-1)^3}, |z| > 3$, then find the value of $f(1)$, $f(2)$ and $f(3)$.

 (b) Evaluate $Z^{-1} \left[\frac{z^2}{(z-1)(z-3)} \right]$ using convolution theorem.

[8+8]
