

Code No: R10206

R10
SET-1
I B. Tech II Semester Supplementary Examinations, Nov/Dec - 2017
MATHEMATICAL METHODS

(Com. to ECE, IT, ME, CHEM. E, BME, E COM. E, PCE, PT & MM)

Time: 3 hours

Max. Marks: 75

 Answer any **FIVE** Questions
 All Questions carry **Equal** Marks
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1. a) Reduce the matrix  $\begin{bmatrix} 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \\ 9 & 10 & 11 & 12 \end{bmatrix}$  in to normal form and then find the rank of the matrix. (7M)

- b) Apply Guass – Seidel method to solve the equations (8M)
- $$\begin{aligned} 27x + 6y - z &= 85 \\ x + y + 54z &= 110 \\ 6x + 15y + 2z &= 72 \end{aligned}$$

2. a) If  $A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -4 & -3 \end{bmatrix}$ , find  $A^{-1}$  using Cayley- Hamilton theorem. (7M)

- b) Find eigenvalues and eigen vectors of  $\begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}$ . (8M)

3. Reduce the quadratic form  $x^2 + 3y^2 + 3z^2 - 2yz$  to canonical form and hence find index and signature. (15M)

4. a) Using the method of false position, find a real root of  $x^6 - x^4 - x^3 - 1 = 0$  correct to three decimal places. (7M)

- b) Using Newton-Raphson method, find a root of  $x^2 + 4 \sin x = 0$  correct to three decimal places. (8M)

5. a) Using Newton's interpolating formula, find  $f(1.85)$ , given the following table (7M)

|      |       |      |      |      |      |       |
|------|-------|------|------|------|------|-------|
| X    | 1.7   | 1.8  | 1.9  | 2.0  | 2.1  | 2.2   |
| F(x) | 5.474 | 6.05 | 6.68 | 7.38 | 8.16 | 9.025 |

- b) Apply Lagrange's interpolating formula to find the value of x when  $f(x)=15$  from the given data (8M)

|      |    |    |    |    |
|------|----|----|----|----|
| x    | 5  | 6  | 9  | 11 |
| f(x) | 12 | 13 | 14 | 16 |

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6. a) Use Trapezoidal to estimate  $\int_0^2 e^{x^2} dx$  taking 10 intervals. (7M)
- b) Evaluate  $\int_0^9 \frac{dx}{1+x^3}$  by Simpson's  $\frac{3}{8}$  th rule. (8M)
7. a) Use Range – Kutta method of order four to find  $y(0.2)$  given that  $10y^1 = x^2 + y^2, y(0) = 1$ . (7M)
- b) Using Milne's method, find  $y(0.4)$ , given  $y^1 = 2e^x - y, y(0) = 2, y(0.1) = 2.01, y(0.2) = 2.04$  and  $y(0.3) = 2.09$ . (8M)
8. Fit a least square curve of the form  $y = ax^b$  for the following data. (15M)

|   |     |     |     |     |     |      |
|---|-----|-----|-----|-----|-----|------|
| X | 0.1 | 0.2 | 0.3 | 0.4 | 0.7 | 1.0  |
| y | 2.4 | 2.9 | 3.7 | 4.1 | 7.8 | 11.2 |

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