

Code No: R10107

R10
SET - 1
I B. Tech I Semester Supplementary Examinations, Oct/Nov - 2018
MATHEMATICAL METHODS

(Com. to CE,CSE,EEE,EIE,AE,BT&AME)

Time: 3 hours

Max. Marks: 75

 Answer any **FIVE** Questions
 All Questions carry **Equal Marks**

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1. a) Find the rank of the matrix  $A = \begin{bmatrix} 1 & 2 & 3 & 0 \\ 2 & 4 & 3 & 2 \\ 3 & 2 & 1 & 3 \\ 6 & 8 & 7 & 5 \end{bmatrix}$  by Echelon form. (7M)
- b) Solve the equations  $x + y + z - w = 2$ ,  $7x + y + 3z + w = 12$ ,  $8x - y + z - 3w = 5$ ,  $10x + 5y + 3z + 2w = 20$ . by Gauss-Jordan method. (8M)
2. a) Verify Cayley Hamilton theorem for  $A = \begin{bmatrix} 1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$ , hence compute  $A^{-1}$  (8M)
- b) Find the Eigen values and Eigen vectors of  $\begin{bmatrix} -1 & 2 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$  (7M)
3. a) Reduce the Q.F  $2x^2 + 2y^2 + 2z^2 - 2xy + 2xz - 2yz$  to the canonical form. (8M)
- b) Find the rank ,index ,signature and nature of the quadratic form  $2yz + 2zx + 2xy$  (7M)
4. a) Find the positive root of  $x^3 - 5x + 3 = 0$  using False position Method. (8M)
- b) Find the positive root of  $xe^x = 1$  using Newton Raphson Method. (7M)
5. a) Find  $f(5.5)$  using Newton's Backward formula for the following table. (8M)

|   |   |   |    |    |     |     |      |
|---|---|---|----|----|-----|-----|------|
| X | 0 | 1 | 2  | 3  | 4   | 5   | 6    |
| Y | 0 | 1 | 16 | 81 | 256 | 625 | 1296 |

- b) Use Lagrange's formula to calculate  $f(8)$  from the following table. (7M)

|   |   |    |    |   |   |    |
|---|---|----|----|---|---|----|
| X | 0 | 2  | 3  | 6 | 7 | 9  |
| Y | 1 | 14 | 15 | 5 | 6 | 19 |

Code No: R10107

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**SET - 1**

6. a) Find the  $f^l(1.4)$  from the following table.

(7M)

|   |      |      |      |      |      |
|---|------|------|------|------|------|
| X | 1    | 1.1  | 1.2  | 1.3  | 1.4  |
| Y | 43.1 | 47.7 | 52.1 | 56.4 | 60.8 |

- b) Evaluate  $\int_0^1 \frac{dx}{1+x^2}$  using (i) Simpson's 3/8<sup>th</sup> Rule (ii) Simpson's 1/3<sup>rd</sup> Rule.

(8M)

7. a) Fit the straight line for the following data.

(7M)

|   |   |    |    |    |    |    |
|---|---|----|----|----|----|----|
| X | 0 | 4  | 8  | 12 | 16 | 20 |
| Y | 6 | 12 | 18 | 24 | 30 | 36 |

- b) Fit the t line  $y = ae^{bx}$  for the following data.

(8M)

|   |     |     |     |     |
|---|-----|-----|-----|-----|
| X | 1.5 | 2.5 | 3.5 | 4.5 |
| Y | 10  | 15  | 20  | 25  |

8. a) By using Runge kutta method of fourth order find  $y(0.1)$  given that

$$\frac{dy}{dx} = 3x + y^2, y(0) = 1$$

- b) By using Picard's method find  $y(0.4)$  given that  $\frac{dy}{dx} = x^2 + y^2, y(0) = 0$

