# II B. Tech II Semester Supplementary Examinations, April-2018 

PROBABILITY AND STATISTICS
(Com. to CSE, IT, CHEM, PE, PCE)

## PART-A

1. a) if X is a normal variate then Find (i) $\mathrm{P}(\mathrm{z}<-1.78)$ (ii) $\mathrm{P}(-0.8<\mathrm{z}<1.53)$
b) The mean and variance of binomial distribution are 4 and 3 respectively.

Find $p(X \geq 1)$.
c) Explain the stratified sampling with a suitable example.
d) A random sample of size 100 has S.D of 5 .what is the maximum error with $95 \%$ confidence
e) Write about major classification of correlation?
f) What is the use of control charts? Draw a typical control chart. $(4 \mathrm{M}+4 \mathrm{M}+3 \mathrm{M}+4 \mathrm{M}+3 \mathrm{M}+4 \mathrm{M})$

## PART-B

2. a) The probability density function of a variate $X$ is

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{X})$ | K | 3 K | 5 K | 7 K | 9 K | 11 K | 13 K |

(i) Find $\mathrm{P}(\mathrm{x}<4), \mathrm{P}(3<\mathrm{x} \leq 6)$.
(ii) What will be the minimum value of K so that $\mathrm{P}(\mathrm{X} \leq 2)>0.3$
b) In a test on 2000 electric bulbs, it was found that the life of a particular make was normally distributed with average life of 2040 hours and S.D of 60 hours . Estimate the number of bulbs likely to burn for
i) More than 2150 hours,
ii) Less than 1950 hours and
iii) More than 1920 hours and but less than 2160 hours.
3. a) Calculate $\mathrm{E}(\mathrm{X}), \mathrm{E}\left(\mathrm{X}^{2}\right), E\left(X-\bar{X}^{2}\right.$ from the distribution given below.

| $X$ | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: |
| $P(X)$ | $1 / 5$ | $3 / 10$ | $1 / 2$ |

b) Define Moment generating function and its properties.
( $8 \mathrm{M}+8 \mathrm{M}$ )
4. a) A random samples of size 25 from a normal population has the mean $\bar{x}=47.5$ and the standard deviation is equal to 8.4. Does this information tend to support or refute the claim that the mean Of population is $\mu=42.5$
b) Three masses are measured as $62.34,20.48,35.97 \mathrm{kgs}$ with S.D $0.54,0.21,0.46 \mathrm{kgs}$ respectively. Find mean and standard deviation of the sum of the masses
( $8 \mathrm{M}+8 \mathrm{M}$ )
5. a) Two independent samples of 8 and 7 items respectively has the following values

| Sample | 11 | 11 | 13 | 11 | 15 | 9 | 12 | 14 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample2 | 9 | 11 | 10 | 13 | 9 | 8 | 10 | ---- |

Is the difference between the mean of samples significant?
b) A sample of 26 bulbs gives a mean life of 990 hours with a S.D of 20 hours.

The manufacturer claims that the mean life of bulbs is 1000 hours is the sample not up to the standard.
6. a) Calculate Karl Pearson's correlation coefficient for the following paired data.

| X | 28 | 41 | 40 | 38 | 35 | 33 | 40 | 32 | 36 | 33 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 23 | 34 | 33 | 34 | 30 | 26 | 28 | 31 | 36 | 38 |

b) Fit a parabola of the form $y=a+b x+c x^{2}$ to the following data
( $8 \mathrm{M}+8 \mathrm{M}$ )

| x | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 23 | 5.2 | 9.7 | 16.5 | 29.4 | 35.5 | 54.4 |

7. Construct a control chart for men and the range for the following data on the basis of fuses, sample of being taken every hour (each set of 5 has been arranged in ascending order of magnitude). Comment on whether the production seems to be under control, assuming that these are the first data.

| 42 | 42 | 19 | 36 | 42 | 51 | 60 | 18 | 15 | 69 | 64 | 61 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 65 | 45 | 24 | 54 | 51 | 74 | 60 | 20 | 30 | 109 | 90 | 78 |
| 75 | 68 | 80 | 69 | 57 | 75 | 72 | 27 | 39 | 113 | 93 | 94 |
| 78 | 72 | 81 | 77 | 59 | 78 | 95 | 42 | 62 | 118 | 109 | 109 |
| 87 | 90 | 81 | 84 | 78 | 132 | 138 | 60 | 84 | 153 | 112 | 136 |

