Code No. 9092

## FACULTY OF MANAGEMENT <br> MBA II - Semester Examination, May/June 2017 <br> Subject: Operations Research <br> Course No. 2.5

Max. Marks: $\mathbf{8 0}$
Time: 3 Hours

$$
\text { PART - A (10x2 = } 20 \text { Marks) }
$$

[Short Answer Type]
Note: Answer all the questions.

1. Explain the following briefly.
a) Characteristics of OR.
b) Non-linear programming
c) Linear programming problem
d) Primal - Dual relationship
e) Travelling salesman problem
f) Restricted assignment problem
g) Assumptions in PERT
h) Total and free floats
i) Queue discipline
j) Pay-off matrix

$$
\text { PART - B ( } 5 \times 12=60 \text { Marks })
$$

[Essay Answer Type]
Note: Answer all the questions using internal choice.
2 a) Define Operations Research (O.R). Explain its nature and give the managerial applications of O.R.

## OR

b) Define general linear programming problem. What are its characteristics? Solve the following L.P. problem graphically:

$$
\begin{array}{ll}
\text { Maximize } z= & 7 x_{1}+3 x_{2} \\
\text { STC } & x_{1}+2 x_{2} \geq 3 \\
& x_{1}+x_{2} \leq 4 \\
& x_{1} \leq \frac{5}{2} \\
& x_{2} \leq \frac{3}{2} \text { and } \\
& x_{1}, x_{2} \geq 0
\end{array}
$$

3 a) Given the L.P. problem solve using simplex method.

$$
\begin{aligned}
\text { Maximization } \mathrm{z}= & 200 \mathrm{x}_{1}+150 \mathrm{x}_{2}+150 \mathrm{x}_{3} \\
\text { STC } & 10 \mathrm{x}_{1}+3 \mathrm{x}_{2}+10 \mathrm{x}_{3} \leq 100 \\
& 5 x_{1}+5 x_{2}+5 x_{3} \leq 60 \text { and } \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{aligned}
$$

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b) Write the dual of the following L.P problem and solve it.

$$
\begin{array}{ll}
\text { Maximize } z= & x_{1}+x_{2}+x_{3} \\
\text { STC } & x_{1}-3 x_{2}+4 x_{3}=5 \\
& x_{1}-2 x_{2} \leq 3 \\
& 2 x_{1}-x_{3} \geq 4 \text { and } \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{array}
$$

4 a) Find an optimal solution to the following transportation problem:

|  | Destination |  |  |  |  |  | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | $\mathrm{D}_{5}$ |  |  |
| $\mathrm{~S}_{1}$ | 5 | 8 | 6 | 6 | 3 | 8 |  |
| $\mathrm{~S}_{2}$ | 4 | 7 | 7 | 6 | 5 | 5 |  |
| $\mathrm{~S}_{3}$ | 8 | 4 | 6 | 6 | 4 | 9 |  |
| Demand | 4 | 4 | 5 | 4 | 8 |  |  |
| OR |  |  |  |  |  |  |  |

b) Find an optimal solution to the following assignment problem.

| - | Job |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | a b | c | d |
| Contractor | 1 | $10 \quad 24$ | 30 | 15 |
| $\square$ | 2 | 1622 | 28 | 12 |
|  | 3 | $12 \quad 20$ | 32 | 10 |
|  |  | 926 | 34 | 16 |

5 a) Determine the maximal flow and the optimum flow in even are for the following network.

www.FirstRanker.com

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b) A small project has the following details:

| Activity | Predecessor | Activity time (days) |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Optimistic | Pessimistic | Likely |
| A | -- | 3 | 11 | 7 |
| B | A | 14 | 28 | 21 |
| C | A | 11 | 17 | 14 |
| D | A, C | 2 | 2 | 2 |
| E | B | 2 | 8 | 3.5 |
| F | D, E | 10 | 21 | 14 |
| G | E, F | 3 | 5 | 4 |
| H | E, F | 4 | 8 | 4.5 |
| I | G, H | 1 | 4 | 2 |

i) Draw the network diagram and compute the expected completion time of the project.
ii) Find the total and free float for non-critical activities.
iii) What is the probability that the length of the project does not exceed 56 days?

6 a) Solve the following game:

$$
\text { Player } A=\left(\begin{array}{ccc}
\text { Player B } \\
10 & 5 & 2 \\
13 & 12 & 13 \\
16 & 14 & 10
\end{array}\right)
$$

## OR

b) Observations of past data show the following patterns in respect of inter arrival durations and service durations in a single channel queuing system. Simulate the queue behaviour for a period of 60 minutes and estimate the probability of the service being idle and the mean time by a customer waiting to be served.

| Inter arrival time |  | Service time |  |
| :---: | :---: | :---: | :---: |
| Minutes | Probability | Minutes | Probability |
| 2 | .15 | 1 | 0.10 |
| 4 | 0.23 | 3 | 0.22 |
| 6 | 0.35 | 5 | 0.35 |
| 8 | 0.17 | 7 | 0.23 |
| 10 | 0.10 | 9 | 0.10 |

Random numbers (Start at North-West corner and proceed along the row)

| 97 | 14 | 72 | 10 |
| :--- | :--- | :--- | :--- |
| 21 | 81 | 87 | 90 |
| 38 | 10 | 29 | 17 |
| 11 | 68 | 99 | 51 |
| 40 | 30 | 52 | 71 |
|  |  |  |  |

