Roll No. $\square$ Total No. of Pages : 02
Total No. of Questions : 08

# M.Tech.(CTM) (Sem.-1) <br> COMPUTATIONAL TECHNIQUES 

Subject Code: CT-503
Paper ID: [E0803]

## Time : 3 Hrs.

Max. Marks : 100

## INSTRUCTIONS TO CANDIDATES :

1. Attempt any FIVE questions out of EIGHT questions.
2. Each question carries TWENTY marks.
3. Assume data suitably if not given.
4. a) Find a root of the following equations using the bisection method correct to two decimal places :
(i) $x^{3}-5 x+1=0($ Root lies between $2 \& 3)$
(ii) $x^{3}-x-11=0($ Root lies between $2 \& 3)$
b) Find cube root of 41 , using Newton-Raphson method.
c) Find negative root of the equation $x^{3}-9 x^{2} \oplus 18=0$ correct to two decimal places by Horner's method.
5. Solve the following equation by the Gauss-Elimination Method:

$$
\begin{aligned}
& 10 x-7 y+3 z+5 \mu=6 \\
& 6 x+8 y-z-4 \mu=5 \\
& 3 x+y+4 z+11 \mu=2 \\
& 5 x-9 y-2 z+4 \mu=7 .
\end{aligned}
$$

3. Find the largest Eigen Value and the corresponding Eigen vector of the matrices :
a) $\left[\begin{array}{lll}1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3\end{array}\right]$
b) $\left[\begin{array}{ccc}1 & 2 & 3 \\ 0 & -4 & 2 \\ 0 & 0 & 7\end{array}\right]$.
4. Solve the elliptic equation $\mathrm{U}_{\mathrm{XX}}+\mathrm{U}_{\mathrm{YY}}=0$ for the square mesh with boundary values as shown in figure. Iterate till the maximum difference between successive values at any point is less than 0.005 .

5. Compute moment ordinates for the beam loaded as under by numerical procedure.

6. a) Find a second degree parabola for the following set of points :

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 2 | 7 | 8 | 10 | 11 | 11 | 10 | 10 | 9 | 8 |

b) Define standard error of estimate.
7. For a trial family of solution as

$$
x=1+c_{1} \cdot t+c_{2} \cdot t^{2}
$$

with $x=1, t=0$

$$
\begin{equation*}
\frac{d x}{d t}=-x, t>0 \text {, evaluate the parameters by applying } \tag{7}
\end{equation*}
$$

(a) Collocation points method
(b) Galerkin method
(c) Least square method.
8. Write short note on :
(a) Explicit solution of non-linear problems.
(b) Coefficient of correlation.

