

**Roll No.**

Total No. of Pages : 01

**Total No. of Questions : 08**

**M.Tech. (ECE) (Sem.-1)**  
**ADVANCED MATHEMATICS FOR ENGINEERS**  
**Subject Code : EC-501**  
**Paper ID : [E0561]**

**Time : 3 Hrs.**

Max. Marks : 100

## **INSTRUCTION TO CANDIDATES :**

1. Attempt any FIVE questions out of EIGHT questions.
  2. Each question carries TWENTY marks.

1. Find the Fourier cosine transform of  $f(x) = \frac{1}{1+x^2}$ . Hence derive Fourier sine transform of

$$\phi(x) = \frac{x}{1+x^2}$$

2. a) Find Z-transform of i)  $C(n + p, p)$  ii)  $n \sin n\theta$   
     b) Find inverse Z-transform of  $\frac{2z^2 + 3z}{(z+2)(z-4)}$ .

3. Find largest eigen values and the corresponding eigen vector of the matrices

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

4. Solve the equation using Gauss-seidal iteration method

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$

5. Use Rayleigh-Ritz method to solve  $y'' + y + x = 0$  ( $0 \leq x \leq 1$ ),  $y(0) = y(1) = 0$ .

6. Under the transformation of  $w = \frac{1}{z}$  find image of  $|z - 2i| = 2$ .

7. State and prove brachistochrone problem.

8. a) State and Prove Convolution theorem for Fourier transforms.  
b) Find relationship between Fourier and Laplace transforms.