

RpifigrVE

USN

15MAT31

Ent*,
Third Semegfer B.E. Degree Examination, Dec.2018/Jan.2019
Engineering Mathematics - III

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing one full question from each module.

Module-1

- 1 a. An alternating current after passing through a rectifier has the form,

$$I = \begin{cases} I_0 \sin x & \text{for } 0 < x < \pi \\ 0 & \text{for } \pi < x < 2\pi \end{cases}$$
 where I_0 is the maximum current and the period is $= 2\pi$. Express I as a Fourier series. (08 Marks)
- b. Determine the constant term and the first cosine and sine terms of the Fourier series expansion of from the following data: (08 Marks)

x	0	45	90	135	180	225	270	315
y	2	1.5	1	0.5	0	0.5	1	1.5

OR

- 2 a. Obtain the Fourier series expansion of the function, $f(x)$ in $-\pi < x < \pi$ and hence deduce that,

$$\frac{1}{12} \pm \frac{1}{32} + \frac{1}{52} \dots = \frac{\pi^2}{8}$$
 (06 Marks)
- b. Find the Fourier series expansion of the function,
 $f(x) = \begin{cases} \pi x & \text{in } 0 < x < \pi \\ \pi(2 - x) & \text{in } \pi < x < 2\pi \end{cases}$ (05 Marks)
- c. The following table gives the variations of periodic current over a period.

t(sec)	0	$\frac{T}{2}$	$\frac{3T}{4}$	$\frac{5T}{4}$	$2T$	$5T$	T
A(amplitude)	1.98	1.30	1.05	1.3	-0.88	-0.25	1.98

Show by harmonic analysis that there is a direct current part of 0.75 amp in the variable current and obtain the amplitude of first harmonic. (05 Marks)

Module-2

- 3 a. Find the complex Fourier transform of the function $f(x) = \begin{cases} 1 & \text{for } -a < x < a \\ 0 & \text{for } x > a \end{cases}$. Hence evaluate $\int_{-\infty}^{\infty} \frac{\sin x}{x} dx$. (06 Marks)
- b. Find the Fourier sine transform of e^{-ax} . (05 Marks)
- c. Compute the inverse z-transforms of $\frac{3z^2 + 2z}{(5z - 1)(5z + 2)}$. (05 Marks)

Important Note

15MAT31

OR

- 4 a. Find the z-transform of $e^n + \sin n$ (06 Marks)
- b. Solve $y_{n+2} + 6y_n + 9y_0 = 2n$ with $y_0 = y_1 = 0$ using z-transform. (05 Marks)
- c. Find the Fourier cosine transform of, $f(x) = \begin{cases} 4x & 0 < x < 1 \\ 4-x & 1 < x < 4. \\ & x > 4 \end{cases}$ (05 Marks)

Module-3

- 5 a. Find the Correlation coefficient and, equations of regression lines for the following data:

x	1	2	3	4	5
y	2	5	3	8	7

(06 Marks)

- b. Fit a straight line to the following data:

x	0	1	2	3	
y	1	1.8	3.3	4.5	6.3

(05 Marks)

- c. Find a real root of the equation $xe^x = \cos x$ correct to three decimal places that lies between 0.5 and 0.6 using Regula-falsi method. (05 Marks)

OR

- 6 a. The following regression equations were obtained from a correlation table.

$$y = 0.516x + 33.73$$

$$x = 0.516y + 32.52$$

Find the value of (i) Correlation coefficient (ii) Mean of x's (iii) Mean of y's.

(06 Marks)

- b. Fit a second degree parabola to the following data:

x	1.0	1.5	2.0	2.5	3.0	3.5	4.0
y	1.1	1.3	1.6	2.0	2.7	3.4	4.1

(05 Marks)

- c. Use Newton-Raphson's method to find a real root of $x \sin x + \cos x = 0$ near $x = \pi$ carry out three iterations. (05 Marks)

Module-4

- 7 a. The following data gives the melting point of an alloy of lead and zinc, where t is the temperature in °C and P is the percentage of lead in the alloy:

P%	60	70	80	90
t	226	250	276	304

Find the melting point of the alloy containing 84% of lead, using Newton's interpolation formula. (06 Marks)

- b. Apply Lagrange's interpolation formula to find a polynomial which passes through the points (0, -20), (1, -12), (3, -20) and (4, -24) (05 Marks)

- c. Find the approximate value of $\int_0^2 \cos x dx$ by Simpson's $\frac{3}{8}$ rule by dividing it into 6 equal parts. (05 Marks)

15MAT31

OR

8 a. From the following table :

x°	10	20	30	40	50	60
$\cos x$	0.9848	0.9397	0.8660	0.7660	0.6428	0.5

Calculate $\cos 25^\circ$ using Newton's forward interpolation formula. (06 Marks)

b. Use Newton's divided difference formula and find $f(6)$ from the following data:

x	5	7	11	13	17
$f(x)$	150	392	1452	2366	5202

(05 Marks)

c. Evaluate $\int_0^1 \frac{dx}{1+x}$ using Weddle's rule by taking equidistant ordinates. (05 Marks)

Module-5

9 a. Find the area between the parabolas $y^2 = 4x$ and $x = 4y$ with the help of Green's theorem in a plane. (06 Marks)

b. Solve the variational problem $\int_0^1 (12xy + y^{12}) dx = 0$ under the conditions $y(0) = 3, y(1) = 6$. (05 Marks)

c. Prove that the shortest distance between two points in a plane is along the straight line joining them. (05 Marks)

OR

10 a. A cable hangs freely under gravity from the fixed points. Show that the shape of the curve is a catenary. (06 Marks)

b. Use Stoke's theorem to evaluate for $F = (x^2 + y^2)j - 2xyk$ taken around the rectangle bounded by the lines $x = \pm a, y = 0, y = b$. (05 Marks)

c. Evaluate $\iiint_S (yzi + zxj + xyk) \cdot \mathbf{r} \, ds$ where S is the surface of the sphere $x^2 + y^2 + z^2 = a^2$ in the first octant. (05 Marks)