B.Tech II Year II Semester (R09) Regular \& Supplementary Examinations, April/May 2013 DESIGN AND ANALYSIS OF ALGORITHMS
(Common to CSS, IT and CSE)
Time: 3 hours
Max Marks: 70
Answer any FIVE questions
All questions carry equal marks

1 (a) Give brief description about performance measurement.
(b) Write an algorithm to implement magic square.

2 (a) Define collapsing rule. Write the algorithm for COLLAPSING FIND by using COLLAPSING RULE.
(b) Draw the different trees for the following sets $S_{1}=\{1,7,8,9\}, S_{2}=\{2,5,10\}, S_{3}=\{3,4,6\}$ with root nodes as 1,5 and 3 .

3 (a) Draw the tree calls of the function merge for the following set of elements:

$$
(5,80,30,20,50,10,70,60,40,90)
$$

(b) Sort the above set of elements by using merge sort.

4 With the help of a suitable example, explain the greedy knapsack.
5 Find the shortest path $\mathrm{b} / \mathrm{w}$ all pairs of nodes in the following graph.


6 (a) Explain how the solution to the backtracking problems is represented. And how it is built.
(b) Give the explicit and implicit constraints in 8 -queens problem.

7 Solve the traveling sales man problem for the following graph by using branch and bound.


Explain about decision and optimization problems with an examples.
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1 (a) Explain the different areas of research where the algorithms can be applied.
(b) Explain how to identify the repeated elements.

2 (a) Explain the scheme to construct bi-connected graph.
(b) What is articulation point? Explain with example.

3 (a) Write an algorithm to sort N numbers in ascending order using merge sort.
(b) Compute the time complexity for merge sort.

4 (a) Present a greedy algorithm for sequencing unit time jobs with deadlines and profits.
(b) Present an optimal randomized algorithm for minimum cost spanning trees.

5 Find the optimal sequence by using traveling sales person for the following given instance.
$\left.\begin{array}{cccc} & \mathrm{A} & \mathrm{B} & \mathrm{C} \\ \mathrm{A} \\ \mathrm{A} \\ \mathrm{B} \\ \mathrm{C} \\ \mathrm{D} & {\left[\begin{array}{c}\alpha \\ 12\end{array}\right.} & 12 & 5 \\ 11 & \alpha & 13 & 6 \\ 4 & 9 & \alpha & 18 \\ 10 & 3 & 2 & \alpha\end{array}\right]$

6 (a) Apply backtracking to the problem of finding a Hamiltonian circuit in following graph.

(b) Write the implementation of the above algorithm.

7 (a) Write FIFOBB algorithm for the 0/1 knapsack problem.
(b) Explain the general method of branch and bound.

8 (a) Prove that if $X \in N P$ y is NP-hard, then $X \leq_{T}^{P} Y$. In other words, NP-hard problems are at least as hard as any problems in NP.
(b) Prove that any two NP-complete problems are polynomially turning equivalent.

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(Common to CSS, IT and CSE)
Time: 3 hours
Max Marks: 70
Answer any FIVE questions
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1 (a) Write Miller-Rabin's primality testing algorithm.
(b) Discuss the different approaches to find the time complexity of algorithm.

2 (a) Give the trees for the set $\{1,2,3,4,5, \ldots n\}$ by using weighting rule.
(b) Give an algorithm for implementation of union instruction using linked list and explain its implementation.

3 (a) Derive the time complexity for strassen's matrix multiplication.
(b) How many additions, multiplications and subtractions are needed for a $2 \times 2$ matrix multiplication?

4 (a) Write a detailed note on job sequencing with deadlines.
(b) Explain in detail about the optimal randomized algorithm for minimum cost spanning trees.

5 (a) How would you construct an optimal binary search tree for a set of $n$ keys if all the keys are equally likely to be searched for? What will be the average number of comparisons in the tree if $n=2^{k}$ ?
(b) Write a pseudo code of the bottom-up dynamic programming algorithm for the knapsack problem.

6 (a) Generate all permutations of $\{1,2,3,4\}$ by backtracking.
(b) Apply backtracking to solve the 3 -coloring problem for the graph of.


7 (a) Explain how the traveling salesperson problem is solved by using LC branch and bound.
(b) Write the general algorithm for branch and bound.

8 Give a dynamic programming solution for the subset sum problem. Analyze the asymptotic order of your solution. Explain why this solution does not put the subset sum problem in NP-hard.
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Time: 3 hours
Max Marks: 70
Answer any FIVE questions
All questions carry $\underset{* * * * *}{\text { equal marks }}$
1 (a) Define an algorithm. Explain the different criteria that satisfy the algorithm.
(b) Briefly explain about asymptotic notations.

2 Explain spanning trees and minimum cost spanning trees with suitable examples.
3 (a) What are the advantages of Strassens' matrix multiplication over normal one?
(b) Present an algorithm for quick sort by using iterative method.

4 (a) Present a general method of greedy technique.
(b) Explain the greedy knap sack with suitable example.

5 (a) Solve the following instance of the ALL PAIRS shortest path problem.

(b) Discuss how to compute the cost of binary search tree.

6 Draw and explain the tree organization of the 4-queen solution space.
$7 \quad$ Solve the TSP problem for the following graph using branch and bound technique.


8 Consider the problem DNF-DISSAT which takes a Boolean formula $S$ in disjunctive normal form (DNF) as input and asks if $S$ is dissatisfiable that is variable of $S$ so that if evaluates to 0 . Show that DNF-DISSAT is Np - complete.

