Set No: 1 **R07** Code No: V3107

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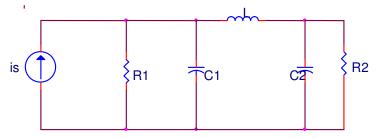
LINEAR SYSTEMS ANALYSIS

(Electrical and Electronics Engineering)

Time: 3 Hours Max Marks: 80

> Answer any FIVE Questions All Questions carry equal marks ****

1. a) Write state equations for the network shown using graph theory.



b) What is state transition matrix? Discuss about its properties.

[8M]

[8M]

- a) Determine the Fourier transform of the unit step, ramp and sinusoidal signals. [12M]
 - b) State and Prove Parseval's Theorem.

[4M]

a) Determine the Fourier transform for the following functions of.

(i)
$$f(t) = t^2 e^{-2t} u(t)$$

(ii)
$$f(t) = e^{-at^2}$$

(iii)
$$f(t) = \frac{2a}{a^2 + t^2}$$

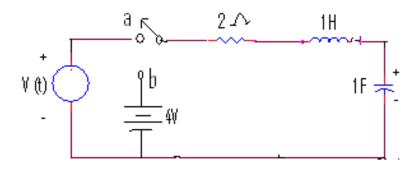
(ii)
$$f(t) = e^{-at^2}$$

(iv) $f(t) = \frac{t^{n-1}}{(n-1)!}e^{-at}u(t)$ [8M]

b) Explain about the power spectrum of the series?

[8M]

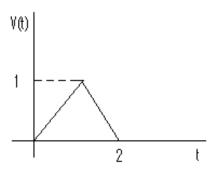
4. a) In the figure shown below the switch is initially at position 'a'. After steady state condition is reached when i(0)=2A and $v_c(0)=2V$. The switch is now thrown to position 'b'. Determine the current in the circuit? [8M]



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b) A triangular wave shown below is applied to a series RL circuit with R= 1 ohm L= 1H. Determine the current i(t) through the circuit. [8M]



- 5. a) Find the range of 'a' so that $H(s)=S^4+S^3+aS^2+2S+3$ is Hurwitz. [8M]
 - b) Test whether the following function is positive real or not? [8M]

$$N(s) = \frac{(S+2)}{(S^2 + 3S + 2)}$$

6. a) Synthesize the Foster II form network when its admittance function is given as. [8M]

$$Y(s) = \frac{S(S^2 + 3)(S^2 + 5)}{(S^2 + 2)(s^2 + 4)}$$

- b) State and explain the properties of LC impedance function. [8M]
- 7. a) Consider a filter with $H(\omega) = \frac{1}{1 + j\omega}$ and input $x(t) = e^{-2t} u$ (t). Find the energy spectral density of the output. [8M]
 - b) Explain about power spectral density. [8M]
- 8. a) Determine the inverse transform of. [8M]

$$X(z) = \frac{3Z^4 - 10Z^3 - 5.75Z^2}{(Z - 1)(Z - 0.5)(Z^2 + 0.25)}$$

b) Define Z-Transform & discuss about the properties of Z- transform. [8M]

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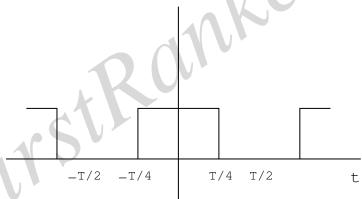
Time: 3 Hours Max Marks: 80

Answer any FIVE Questions
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1. a) A system is described by a third order differential equation $\ddot{x} + 9\ddot{x} + 26\dot{x} + 24x = 12u(t)$. Where x is the output and u (t) is the input. Obtain the state space representation of the system. [8M]

b) Determine the state transition matrix for the matrix $A = \begin{bmatrix} 3 & 0 & 0 \\ 0 & -2 & 1 \\ 0 & 4 & 1 \end{bmatrix}$ [8M]

2. a) Determine the Fourier coefficients a_n & b_n of the waveform shown in the fig. having an 'ON' period = 'OFF' period =T/2. The waveform is a rectangular pulse train with 50% duty cycle. [8M]



b) Determine the Fourier transform of the Signum function.

- [8M]
- 3. A 2Ω resistive load is supplied from a full wave rectifier connected to 230 V, 50 Hz single phase supply. Determine the average and RMS values of load current. Hence determine the proportion of DC power & AC power to the total power in the load. Investigate the effect of adding an inductance in series with the load.
- 4. a) A series RL circuit experiences an exponential voltage $v = 10e^{-100t}$ after closing a switch at t=0 assume R=1 Ω L=0.1 H [8M]
 - b) Current I(s) in a network is given by $I(s) = \frac{2S+3}{S^2+3S}$. Find i(t), the current at any time t.

[8M]

5. a) Check whether the polynomial S⁴ +S³ +5S² +3S+4 is Hurwitz or not [10M] b) State and explain the properties of positive real function. [6M]

6. An impedance function is given by $Z(s) = \frac{(S+1)(S+4)}{S(S+2)(S+5)}$. Find the R-C representation of Cauer-I and II forms. [16M]

7. a) Compare energy spectral density with power spectral density function. [8M] b) Define cross-correlation function and explain the properties of it. [8M]

8. a) What are the differences between continuous time signal & discrete time signal? [8M]
b) Determine Z-Transform of functions x (t) =sinωt and x (t) =cosωt. [8M]

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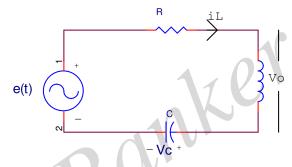
LINEAR SYSTEMS ANALYSIS

(Electrical and Electronics Engineering)

Time: 3 Hours Max Marks: 80

Answer any FIVE Questions All Questions carry equal marks *****

- 1. For the R-L-C circuit shown in fig. the output is the voltage across the inductance. Determine the output for [16M]
 - (i) $i(0)=0, v_c(0)=10$ and e(t)=0
 - (ii) $i(0)=1, v_c(0)=0$ and e(t)= unit step
 - (iii) $i(0) = v_c(0) = 0$ and e(t) = unit impulse



- 2. a) State the relation between the trigonometric & the exponential Fourier series.
- [8M]
- b) Sketch the waveform of a periodic function whose Fourier series has.
 - (i) Only odd harmonics but both sine & cosine terms are present.
 - (ii) Only even harmonics but both sine & cosine terms are present.
 - (iii) Only sine terms but all harmonics are present.
 - (iv) Only cosine terms but all harmonics are present.

[8M]

- 3. A periodic voltage v (t) is applied to the input terminal of a series RLC circuit shown in the figure a. Determine the current i(t) & sketch the line spectra and power spectra. [16M]
 - (i) A triangular periodic signal as shown in fig. **b** but with 1 sec
 - (ii) A rectified sine wave in fig. c

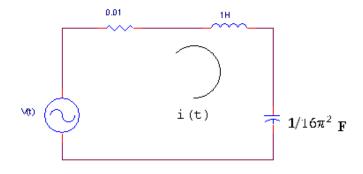
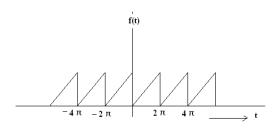


Fig. a

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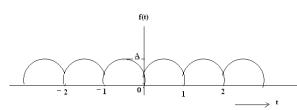


Fig. b

fig. ci

- a) The current through a circuit element is $\frac{4S^2}{S+7}$ Find the current in t-domine as $S \to 0$, $S \to \infty$. Discuss about the nature of circuit elements. [8M]
 - b) A step voltage of 10 volts is applied at t=0 in a series RC circuit where R= 1 Ω and C=2 Farads. Initial charge of a capacitor is nil. Using Laplace transform find i(t). [8M]
- a) State and explain the properties of Hurwitz polynomial. [8M]
 - b) Check whether the function $N(s) = \frac{(S+2)(S+4)}{(S+1)(S+3)}$ is positive real or not. [8M]
- a) Synthesize the network whose driving impedance is given by $Z(s) = \frac{6S^2 + 3S^2 + 2S + 1}{6S^3 + 3S}$
 - b) An impedance function is given by $Z(s) = \frac{(S+1)(S+4)}{S(S+2)(S+5)}$

Find R-L representation of Foster-I and II forms

[8M+8M]

- a) Discuss about the principle of flat top sampling with neat schematics. [8M]
 - b) Find the auto-correlation function of the sine signal expressed as below

 $x(t)=A \sin(\omega t+\varphi)$, where $\omega=2\pi/T$ [8M]

- a) Find inverse Z-transform of the following function $H(Z) = \frac{-4 + 8Z^{-1}}{1 + 6Z^{-1} + 8Z^{-2}}$ using partial fraction method. [8M]
 - b) Determine the Z-transform of the ramp sequence x(n)=An and the sequence $x(n) = Anr^n$

[8M]

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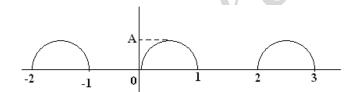
- 1. a) Explain the modeling process of linear systems by means of a specific example. [8M]
 - b) A system is described by a third order differential equation $\ddot{x} + 7\ddot{x} + 14\dot{x} + 8x = u(t)$.

Develop state space representation where the system matrix is a diagonal one. [8M]

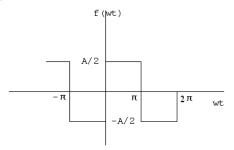
2. a) Explain the exponential form of Fourier series.

[8M]

b) Find the complex Fourier coefficients for the half wave rectified signal shown in the fig. Function f(t) has a period T=2 sec & frequency, $\omega=2\pi/T=\pi$ [8M]



3. Determine the Fourier coefficients for the rectangular waveform shown in fig using graphical method. [16M]



- 4. a) Determine the laplace transform expressions for the following
 - (i) A voltage defined by v(t) = 10 u(t)-10 u(t-2)
 - (ii) Current defined by $i(t) = e^{-(t-2)}$

If the above quantities refer to a circuit determine its components.

[8M]

b) A 10 V step voltage is applied across a RC series circuit at t=0. Find i(t) at t=0⁺ and obtain the value of di/dt at t=0⁺. Assume R= $100 \Omega C=100 \mu F$. [8M]

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- 5. a) Test the function $Z(s) = \frac{S^2 + 7}{(S+1)^3}$ for positive realness. [8M]
 - b) Check whether the polynomial $S^4 + S^3 + 7S^2 + 4S + 6$ is Hurwitz or not [8M]
- The driving point impedance of a one port reactive network is given by

$$Z(s) = \frac{4S(s^2 + 4)}{(S^2 + 1)(S^2 + 16)}.$$
 Obtain the Foster forms of LC network realization. [16M]

- a) Define auto-correlation. Explain the auto correlation of a periodic waveform. [8M]
 - b) State & explain the Sampling theorem. [8M]
- a) The Z-transfer function of a system is given as $H(Z) = \frac{1}{Z^2 \frac{1}{2}Z + \frac{1}{8}}$. Detrmine its discreet

unit step response assuming the system to be initially relaxed. [8M]

b) Determine Z-transform of
$$X(s) = \frac{a}{(S^2 - a^2)}$$
.
