



II B. Tech I Semester, Supplementary Examinations, Nov - 2012 PROBABILITY THEORY AND STOCHASTIC PROCESSES

(Com. to ECE, ECC)

Time: 3 hours

Max. Marks: 80

Answer any FIVE Questions All Questions carry Equal Marks

a) Distinguish between Joint probability and conditional probability. 1.

b) State and Prove the Baye's Theory

c) A box of 30 diodes is known to contain 5 defective ones. If two diodes are slaved at random without replacement, what is the probability that at least one of these diodes is defective?

- a) Define the probability density function of random variable and state its properties 2. b) Explain the Rayleigh distribution and density functions. nke
- 3. a) A random variable has pdf

$$f_{y}(x) = \frac{5}{4}(1 - x^{4}) \qquad 0 \le x \le 1$$
$$= 0 \qquad \text{else where}$$

Find E (4x+2) and E(x^2)

b) Find the characteristic function of the random variable x having the density function.

$$f_x(x) = \frac{1}{2a} |\mathbf{x}| < a$$
$$= 0 \text{ other wis}$$

a) Determine the constant b such that the function 4.

$$f_{XY}(x, y) = 3xy \qquad 0 < x < 1, \qquad 0 < y < b$$
$$= 0 \qquad \text{other wise}$$

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is a valid joint density function

b) Find the density of w=x+y where the densities of x and y are assumed to be

$$f_{X}(\mathbf{x}) = [u(x) - u(x-1)]$$

$$f_{Y}(\mathbf{y}) = [u(\mathbf{y}) - u(\mathbf{y} - 1)]$$

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5. a) Random variable X and Y have the joint density.

$$f_{xy}(x, y) = \frac{1}{24} \qquad 0 < x < 6, \qquad 0 < y < 4$$
$$= 0 \qquad else where$$

What is the expected value of the functions $g(x,y) = (xy)^2$

b) Random variable x_1 and x_2 have the joint Characteristic function

$$\phi x_1, x_2(w_1, w_2) = \left[(1 - j2w_1)(1 - j2w_2) \right]^{-N}$$

Where N>0 is an integer Find the correlation and moment's m₂₀ and m₀₂

- 6. a) Explain the following: i) concept of Stationarity ii) Ergodic Random processes.b) State and prove the properties of Auto correlation function.
- 7. a) If the Auto Correlation of random binary transmission process is given by

$$R(\tau) = \begin{cases} 1 - \frac{|\tau|}{T} & |\tau| \le T \\ 0 & \text{else where} \end{cases}$$

Find the power spectral density of process

- b) Write short notes on "power density spectrum".
- 8. a) A random noise x(t) having the power spectrum $S_{XX}(w) = \frac{3}{49 + w^2}$ is applied to a network

for which $h(t)=u(t) t^2 exp(-7t)$. The network response is denoted by y(t)

i) What is the average power in x(t)

ii) Find the power spectrum of x (t)

- iii) Find the average power of y (t)
- b) Write short notes on "Arbitrary Noise Sources".





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- 1. a) Explain the following in brief
 - i) Probability as a relative frequency
 - ii) Joint provability
 - iii) Baye's theorem
 - iv) Independent events
- b) A multi channel microwave link is to provide telephone communication to a remote community having 12 subscribes, each of whom uses the link 20% of time during peak hours. How many channels are needed to make the line available during peak hours to
 - i) Eighty percent of the subscribes all of the time
 - ii) All of the subscribes 80% of the time
 - iii) All of the subscribes 95% of the time
- 2. a) Find the value of the constant K so that

$$f_x(x) = \begin{pmatrix} Kx^2(1-x^3) & 0 \le x \le 1\\ 0 & \text{other wise} \end{cases}$$

Is this a proper density function of a continuous random variable.

b) Explain about the Gaussian distribution and density function.

a) Find the moment generating function about the origin of the Poisson distribution.
b) Show that any characteristic function q_x (w) satisfies

$$\left|q_{x}(w)\right| \leq q_{x}(0) = 1$$

4. a) Let X and Y be jointly continuous random variables with joint pdfs

$$fXY(x, y) = x^{2} + \frac{xy}{3} \text{ for } 0 \le x \le 1, \quad 0 \le y \le z$$
$$= 0 \qquad \text{other wise}$$

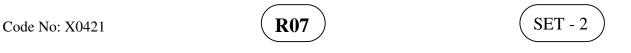
i) Are x and y independent

ii) Check f(x/y) and f(y/x) are pdfs or not

b) State and prove the centered limit theorem.

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5. a) A joint density is given as

$$f_{XY}(x, y) = \begin{cases} x(y+1.5) & 0 < x < 1 \text{ and} \\ 0 & other \text{ wise} \end{cases}$$

Find all the joint moments m_{nk} . n and k=0,1,....

- b) Let x be random variable with E(x)=2 and var (x)=3 verify that random variable x and the random variable y=-4x+8 are orthogonal.
- 6. a) Consider a random process $x(t)=A \cos (\omega t + \theta)$ where w and θ are constants and A is a random variable with zero mean and variance σ_A^2 . Determine whether x(t) is a wide sense stationary process or not

b) Distinguish between Auto correlation function and cross correlation function. State the properties of cross correlation function.

7. a) A stationarity random process has an auto correlation function of

 $R_x(\tau) = 16 - e^{-5|\tau|} \cos 20\pi\tau + 8\cos 10\pi\tau.$

i) Find the variance of this process

ii) Find the spectral density of this process

b) Prove that the power spectrum and Autocorrelation function of the random process form a Fourier Transform pair.

8. Write short notes as: i) Thermal Noise ii) Properties of band limited processes

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1. a) Explain the following

i) Axioms of probability ii) Independent events iii) Total probability

b) A and B are events such that $p(A \cup B) = \frac{3}{4}p(A \cap B) = \frac{1}{4}$ and $P(\overline{A}) = \frac{2}{3}$ find $p(\overline{A}/B)$

c) In a group of external number of men and women 10% men and 45% women are unemployed. What is the probability that a person selected at random is employed?

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2. a) If the communicative distribution function of a random variable x is given by

$$f_{X}(x) = \begin{pmatrix} 1 - \frac{4}{x^{2}} & x \ge 2\\ 0 & x \le 2 \end{pmatrix}$$

Find i) p(x<3) ii) p(4<x<5) iii) p(x≥3)b) Explain about Poisson distribution and density functions.

3. a) Let x be a random variable with distribution f_x given by

$$f_{X}(x) = \begin{pmatrix} 1 - e^{-\lambda x} & 0 \le x \le \infty \\ 0 & other \ wise \end{cases}$$

Find the pdf of x. Determine the mean and variance of the distribution.

b) Find the moment generating function (MGF) for the distribution $f_x(x) = \frac{1}{2^x} x = 1, 2, 3, \dots$ Also find its mean.

4. a) The pdf is given by

$$f_{XY}(x, y) = \frac{6}{5}(x + y^2) \quad 0 \le x \le 1, \quad 0 \le y \le 1$$

= 0 other wise

i) Find the marginal pdf of x and that of y

ii) Find $p\left[\frac{1}{4} \le y \le \frac{3}{4}\right]$

b) Explain about conditional distribution and density internal conditioning.

5. a) Let(x,y) be two dimensional random variable described by joint pdf.

$$f_{XY}(x, y) = 8xy \quad 0 \le x \le 1, \quad 0 \le y \le x$$

= 0 else where
Find the cos (x,y)
b) Explain about "jointly Gaussian random variables"

- 6. a) Discus the stationarity of the random process $x(t) = A\cos(Wot + \theta)$ where A and Wo are constants and θ is a uniformity distributed random variable in $(0, 2\pi)$ b) Consider two random processes $x(t)=3 \cos(wt+\theta)$ and $y(t)=2 \cos(wt+\theta-\pi/2)$ where θ a random variable distributed in $(0, 2\pi)$ prove that $|R_{xy}(\tau)| \le \sqrt{R_{xx}(0)R_{yy}(0)}$
- 7. a) The psd of a random process is given by

$$S_{xx}(w) = \begin{cases} \pi & |w| < 1\\ 0 & else where \end{cases}$$

Find its Auto correlation function

b) What is cross power density spectrum? State its properties

8. a) Find the output power density spectrum and output Auto correlation function for a system with

 $h(t) = e^{-t}$ $t \ge 0$ for as input with $psd = \frac{ho}{2}$ $-\infty < t < \infty$

b) Write short notes on "effective noise temperature".

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- 1. a) Define the following and give are example for each of the following
 - i) Discrete and continuous sample space
 - ii) Mutually Exclusive event
 - iii) Equally likely event

b) A letter is known to have come either from LONDON or CLIFTON. On the post card only two consecutive letters as 'ON' are legible what is the chance that it came from LONDON.c) What is the probability that a randomly selected integer chosen from the first 100 positive integers is odd?

10 Integers is out: 2. a) The distribution for x is defined by $f_X(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 - \frac{1}{4}e^{-x} & \text{for } x \ge 0 \end{cases}$

Determine p(x=0) and p(x>0)

b) Explain about "Binominal distribution and density functions"

3. a) A continuous distribution is given by $\begin{aligned} f_x(x) &= \frac{1}{x\sqrt{2\pi}} e^{-(\log x)^2} \quad x \ge 0 \\ &= 0 \end{aligned}$

Find the mean, standard deviation, coefficient of skewness of this distribution

b) The characteristic function for a Gaussian random variable x, having R mean value of zero is

 $q_{X}(w) = \exp \left|-j\sigma^{2}w^{2}/2\right|$) Find all the moments of x using $q_{X}(w)$

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4. a) The joint pdt of the two dimensional r.v(x,y) is given by

$$f_{xy}(x, y) = \frac{1}{4} e^{|x| - |y|} \qquad -\infty < x < \infty$$
$$-\infty < y < \infty$$
$$= 0 \qquad else where$$

i) Check whether x and y are independent

ii) p(x
$$\leq$$
1, y \leq 0)

Code No: X0421

b) The probability density function of two statistically independent random variables X and Y are

$$f_x(x) = \begin{cases} \frac{3}{32} & (4 - x^2) & -2 \le x \le 2 \\ = 0 & \text{else where in } x \end{cases}$$

$$fy(y) = \frac{1}{2} [x(y+1) - u(y-1)]$$

Find the exact probability density of the sum w=x+y

5. a) Two random variable have a uniform density on a circular region defined by

$$f_{xy}(x, y) = \frac{1}{\pi r^2} x^2 + y^2 \le r^2$$
$$= 0 \qquad else \ where$$

Find the mean value of the function $g(x,y)=x^2+y^2$

b) Two random variables x and y have the joint characteristic function

$$q_{xy}(w_1, w_2) = \exp\left(-2w_1^2 - 8w_2^2\right)$$

Show that i) x and y are both zero mean random variable ii) x and y are uncorrelated

- 6. a) Explain the following w.rto Random processes
 i) Strict sense stationary
 b) Explain about Poisson Random processes
- 7. a) For a random process x(t), assume that $Rxx(\tau) = \rho e^{-\tau^2/2a^2}$ where $\rho > 0$ and a > 0 are constants. Find the power density spectrum of x(t) b) Prove that the cross power spectrum and cross correlation function of Random process form a Fourier transform pair.
- 8. a) Define a given system and derive a relation between the input and output spectra of the system.
 - b) Explain "Resistive noise" in detail.

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